



SIXTH FRAMEWORK PROGRAMME, PRIORITY 1.6
«Sustainable energy systems»

Project: ENhanced Geothermal Innovative Network for Europe
ENGINE

ВУЛКАН

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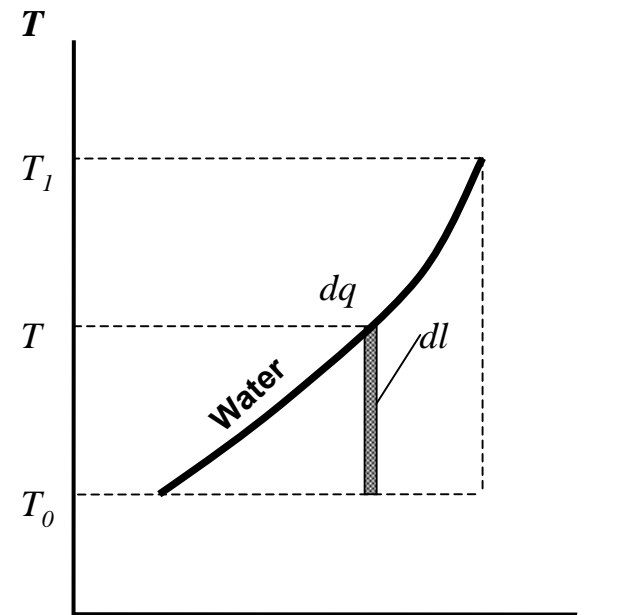
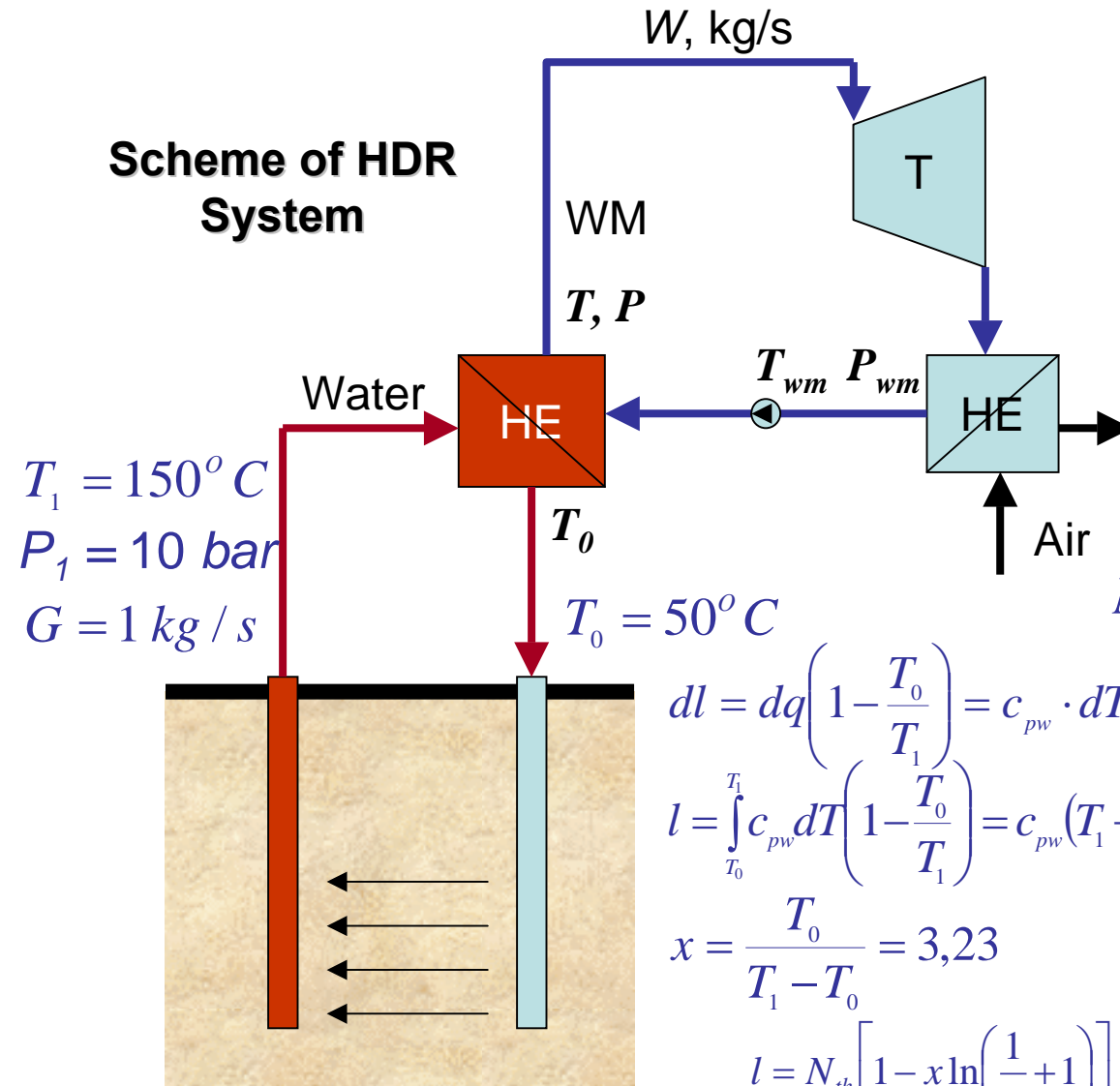
**POWER EXTRACTION FROM
HDR SYSTEMS**

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Scheme of HDR System



$$N_{th} = c_{pw} (T_1 - T_0) = 420 \frac{\text{kW}}{\text{kg/s}} \text{ s}$$

$$dl = dq \left(1 - \frac{T_0}{T_1} \right) = c_{pw} \cdot dT \cdot \left(1 - \frac{T_0}{T_1} \right)$$

$$l = \int_{T_0}^{T_1} c_{pw} dT \left(1 - \frac{T_0}{T_1} \right) = c_{pw} (T_1 - T_0) - c_{pw} T_0 \cdot \ln \frac{T_1}{T_0} = N_{th} \left[1 - \frac{T_0}{T_1 - T_0} \ln \left(\frac{T_1 - T_0}{T_0} + 1 \right) \right]$$

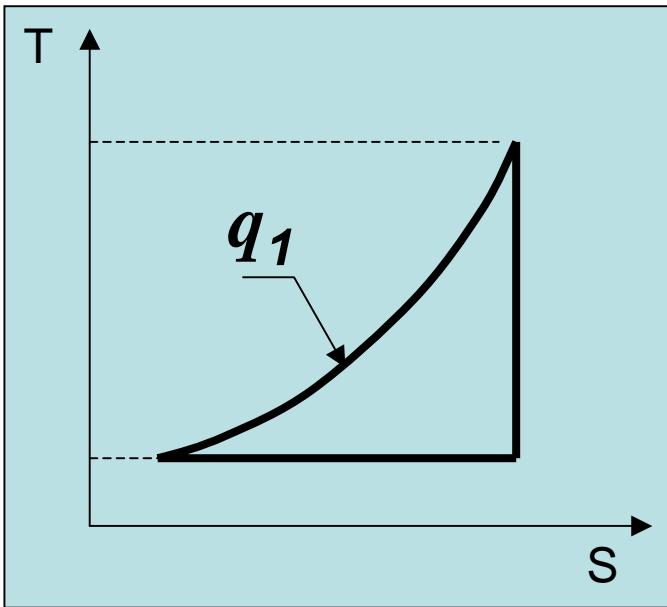
$$x = \frac{T_0}{T_1 - T_0} = 3,23$$

$$l = N_{th} \left[1 - x \ln \left(\frac{1}{x} + 1 \right) \right] = N_{th} (1 - 0,872) \approx 0,128 N_{th}$$

$$\eta_{\max} = \frac{l}{N_{th}} = 12,8\%$$

The thermal power of the water flow is transmitted to a working media (**WM**).

The optimal thermodynamic cycle should have the heat admission curve (in most cases an isobar) which shape is similar to the water cooling down curve shape: constant heat capacity along the heat admission isobar.



Since generally $C_{pwm} \neq C_{pw}$, the specific **WM** flow rate in the heat exchanger should be

$$W = C_{pw} / C_{pwm}$$

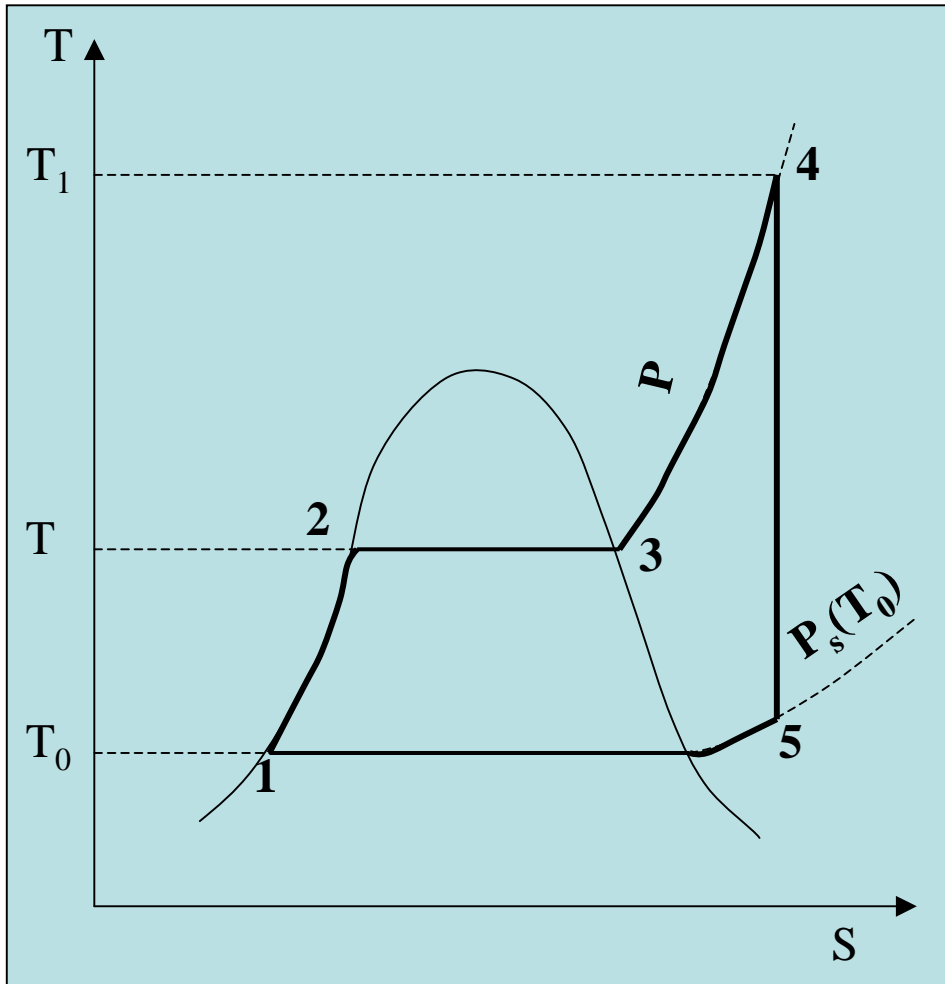
The specific work l , kJ/kg of the WM cycle is

$$l = q_1 \times \eta_t$$

Hence the total installation power $N [\text{kW}] = l [\text{kJ/kg}] \times W [\text{kg/s}]$

In a real cycle $C_{pwm} \neq \text{const}$, there arises a problem with **WM** flow rate.

SUBCRITICAL RANKINE CYCLE

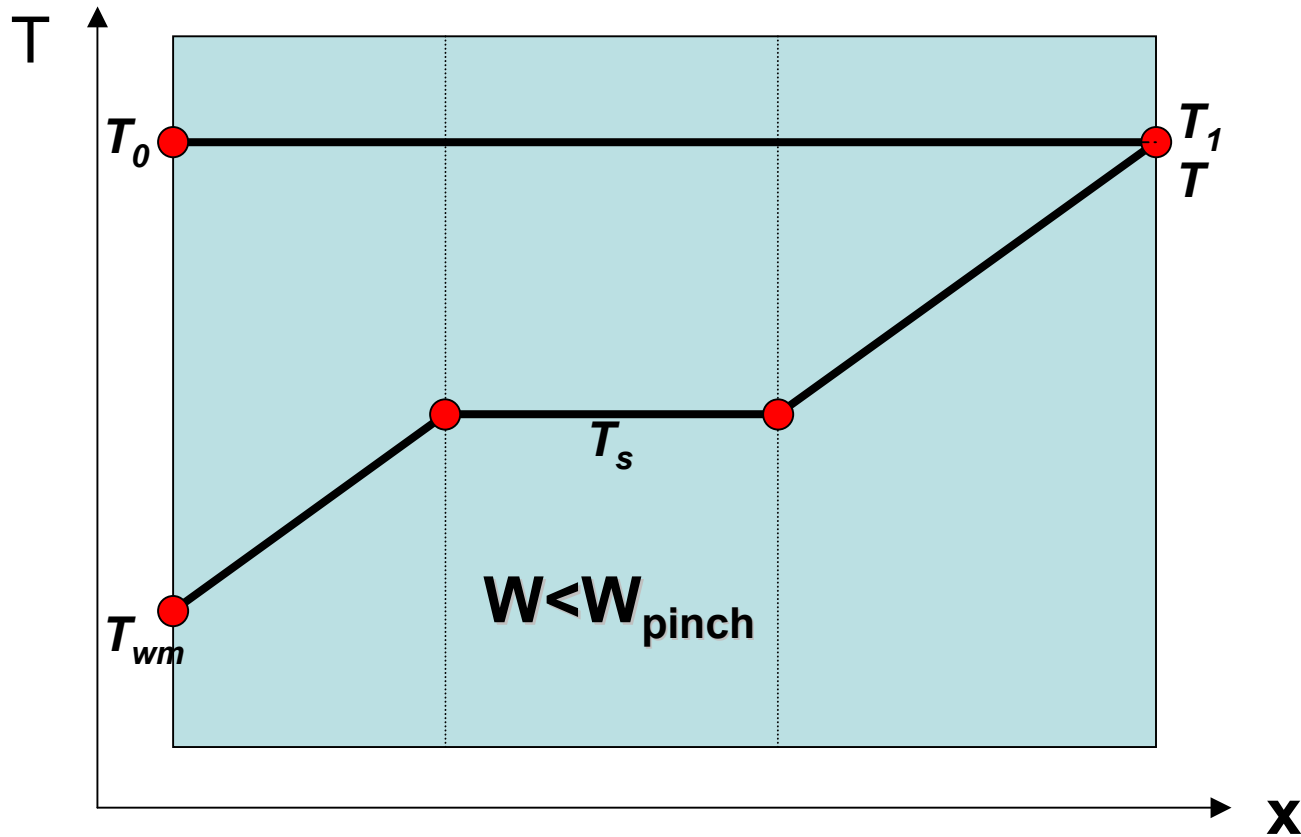


$$q_1 (\text{kJ} / \text{kg}) = (h_4 - h_1)$$

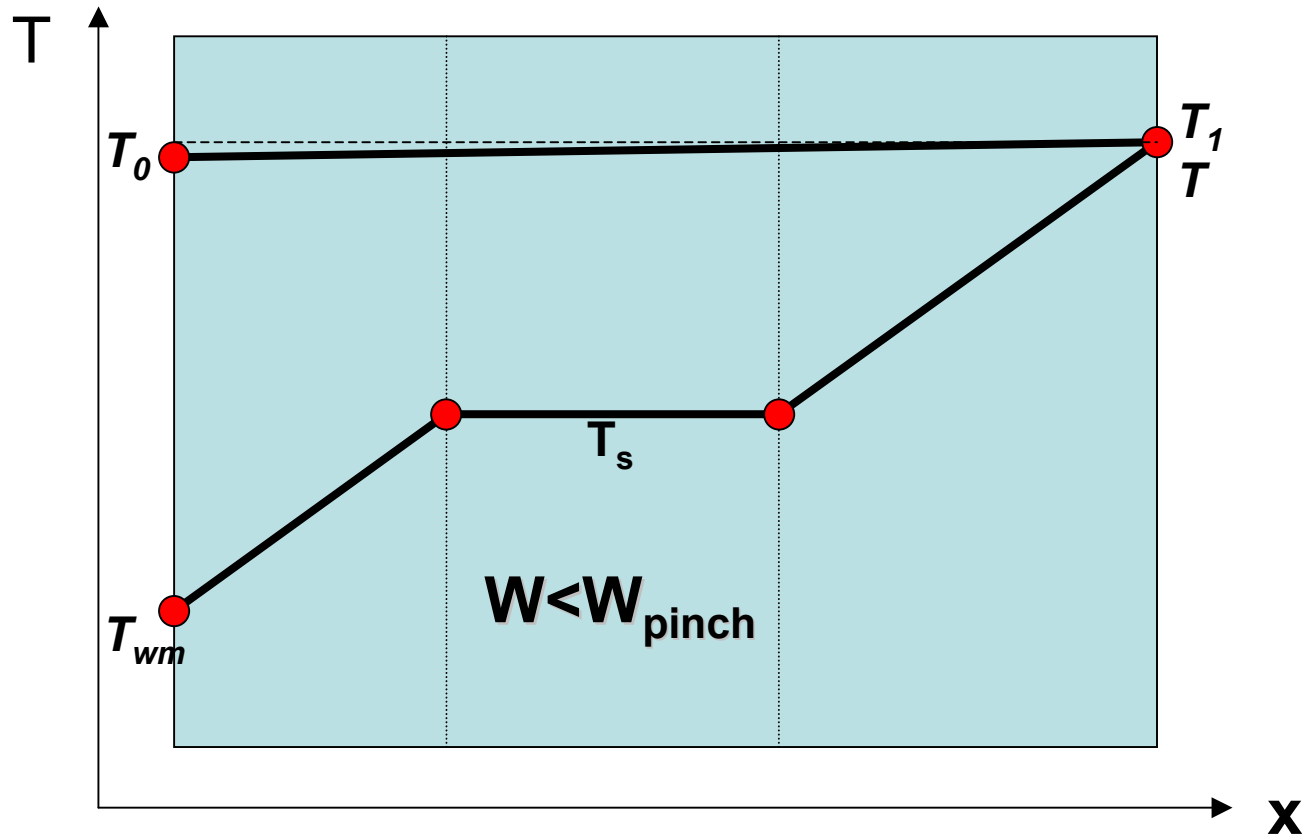
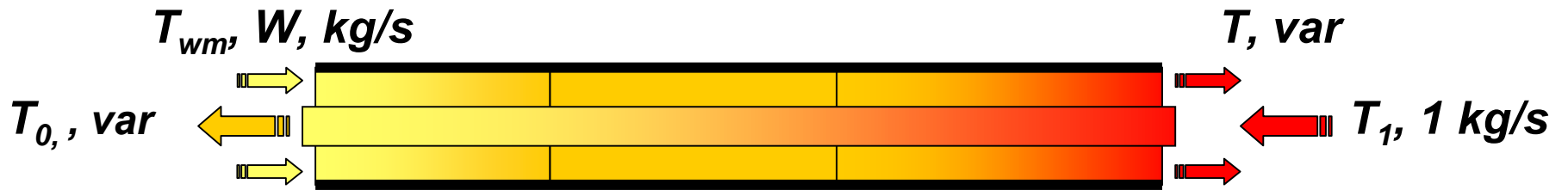
$$l (\text{kJ} / \text{kg}) = (h_4 - h_5)$$

$$\eta_t = l / q_1 = (h_4 - h_5) / (h_4 - h_1)$$

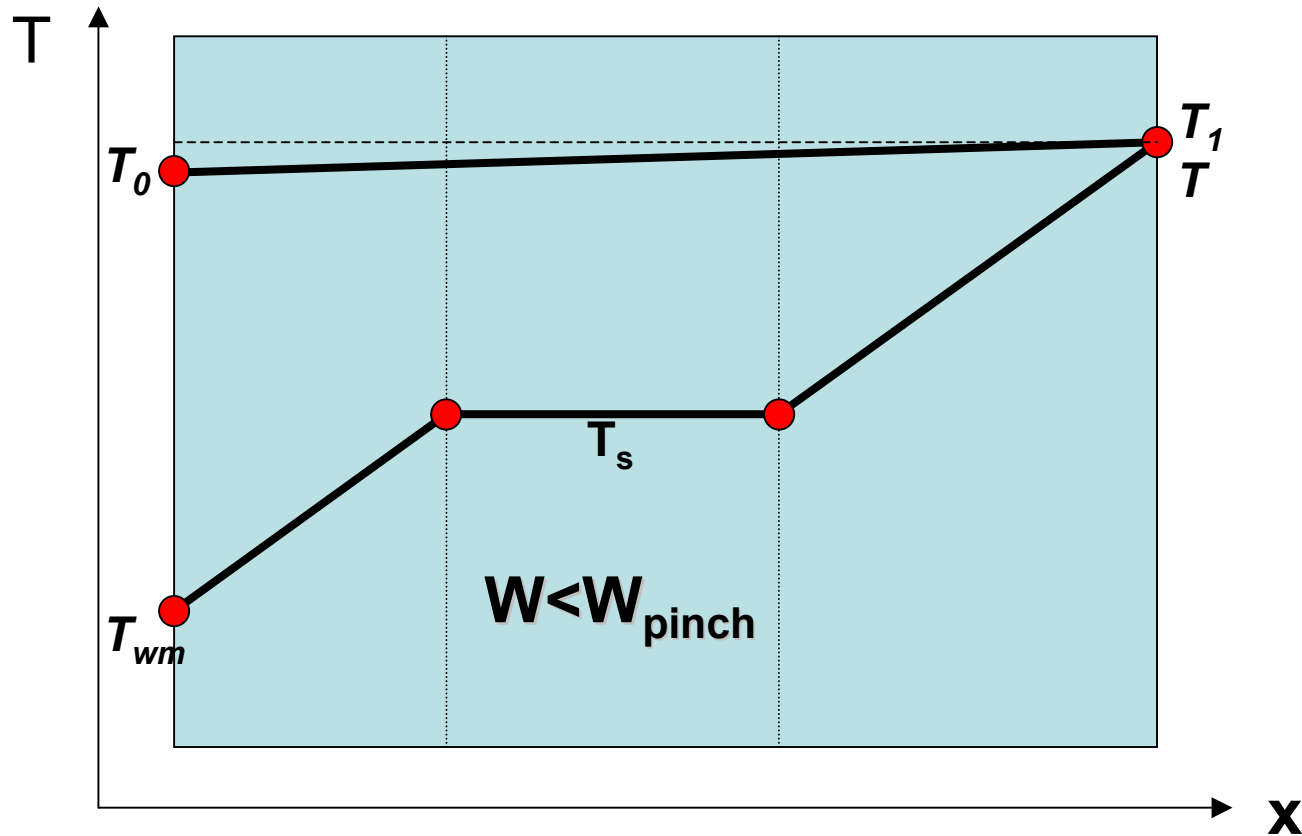
TEMPERATURE PINCH EFFECT IN HEAT EXCHANGER



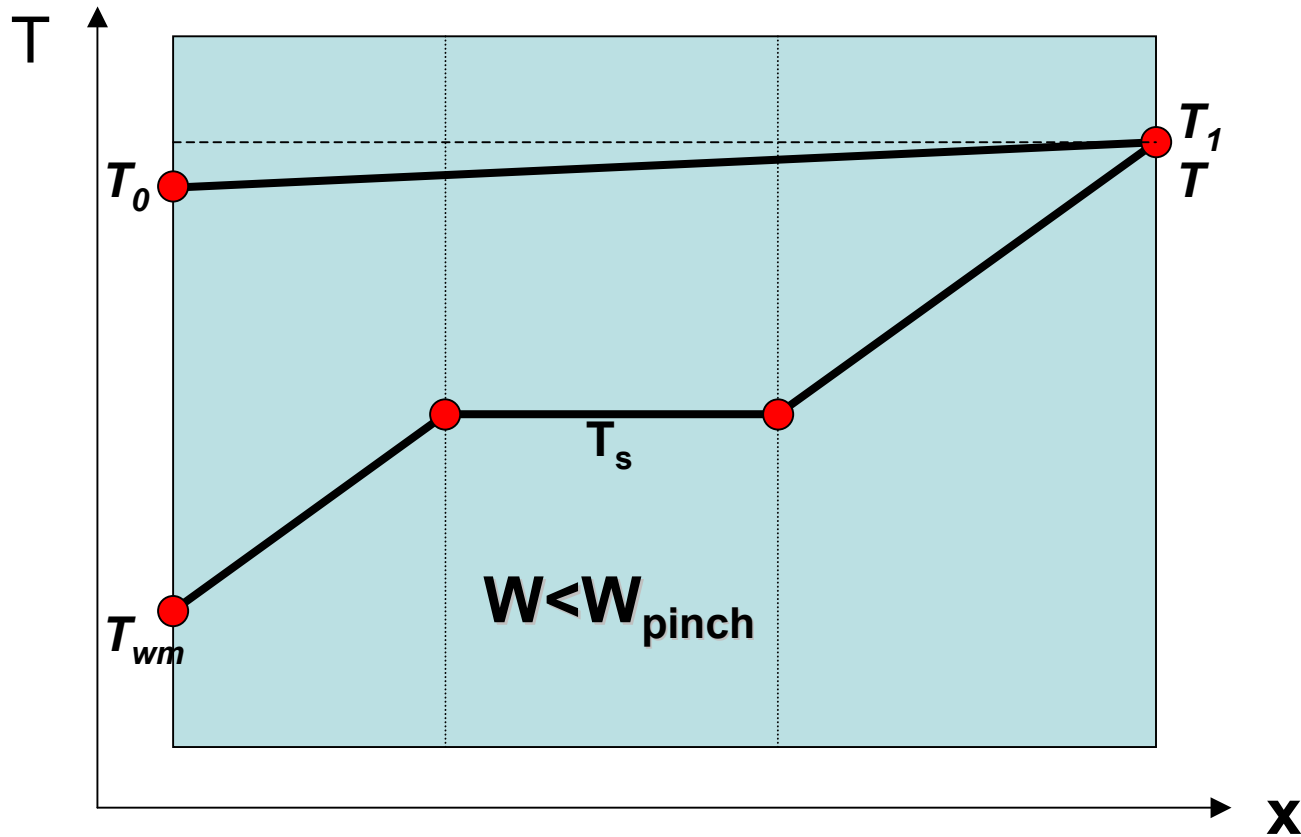
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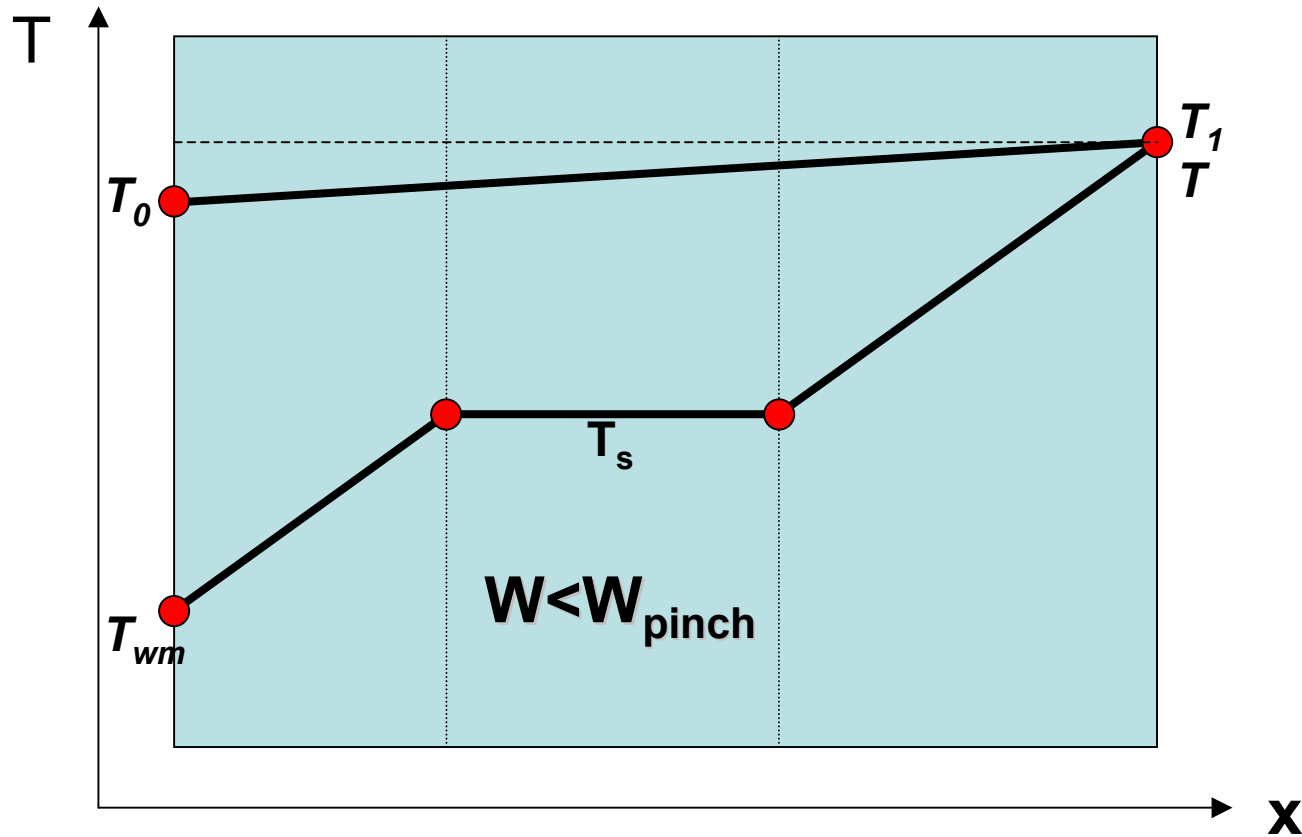
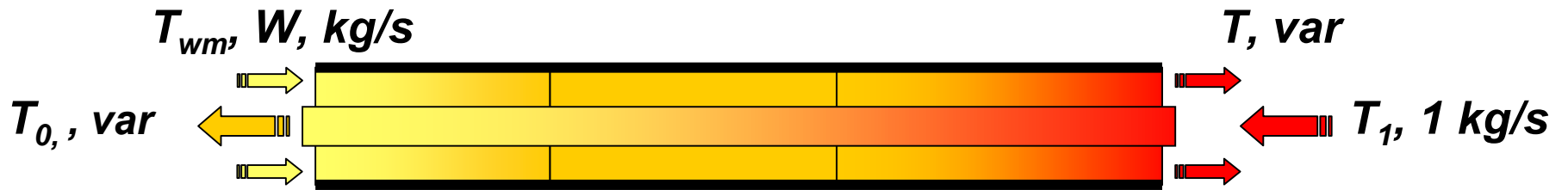
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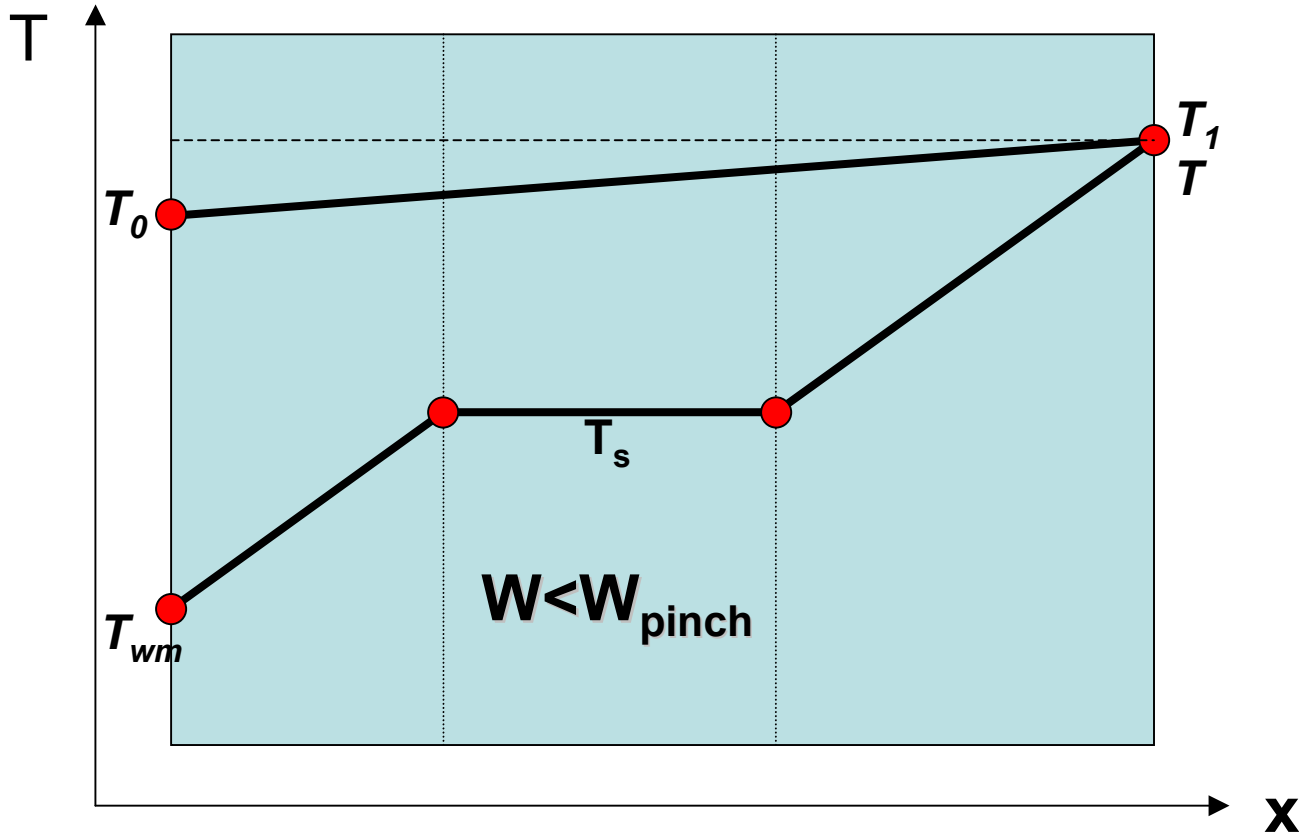
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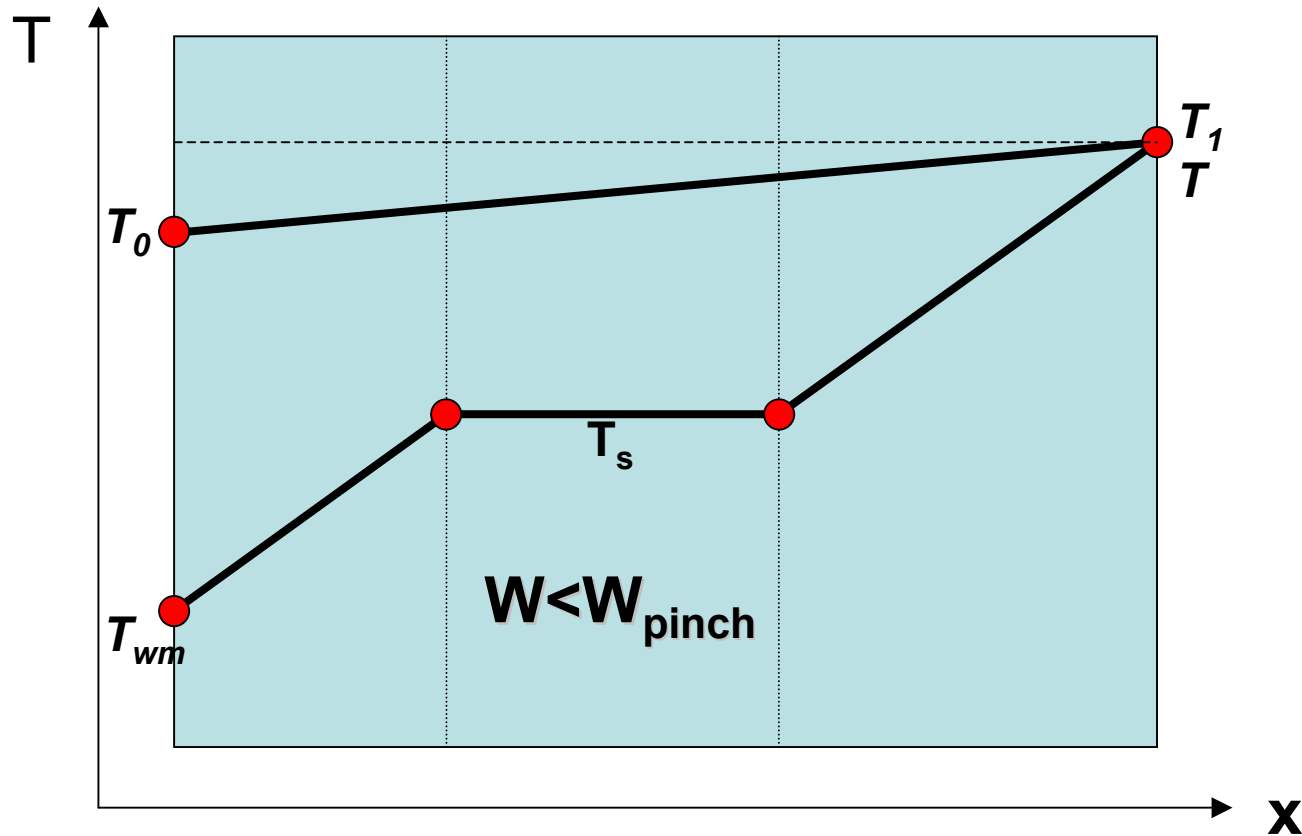
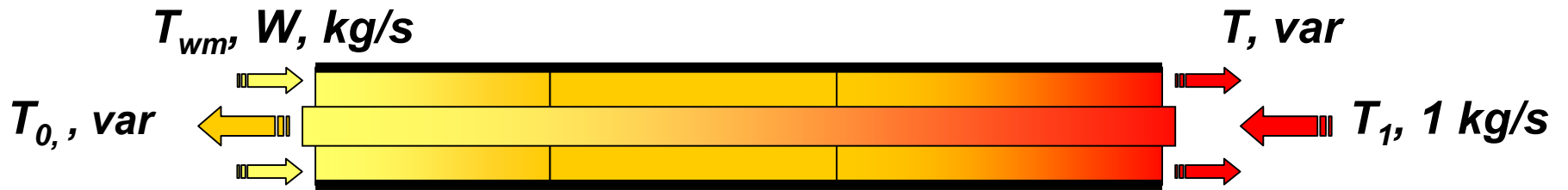
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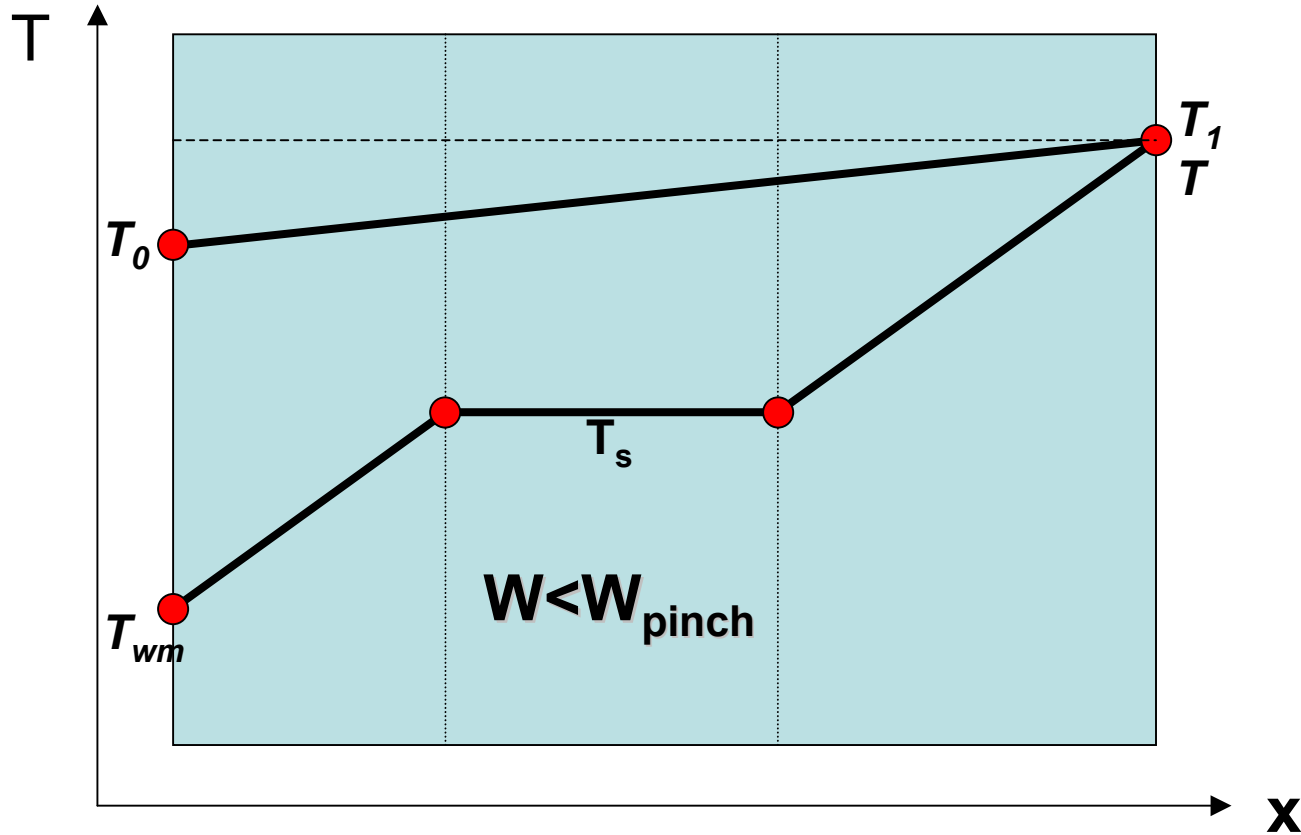
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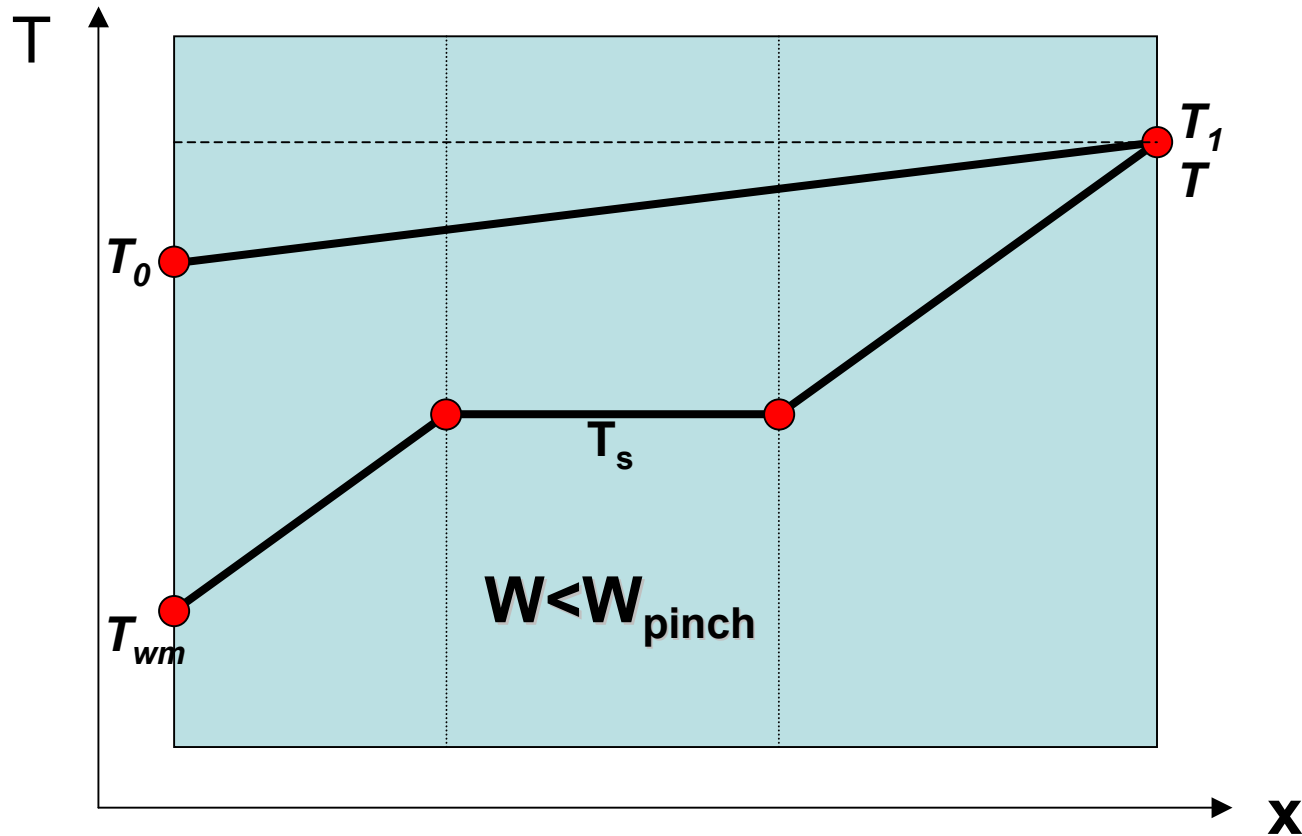
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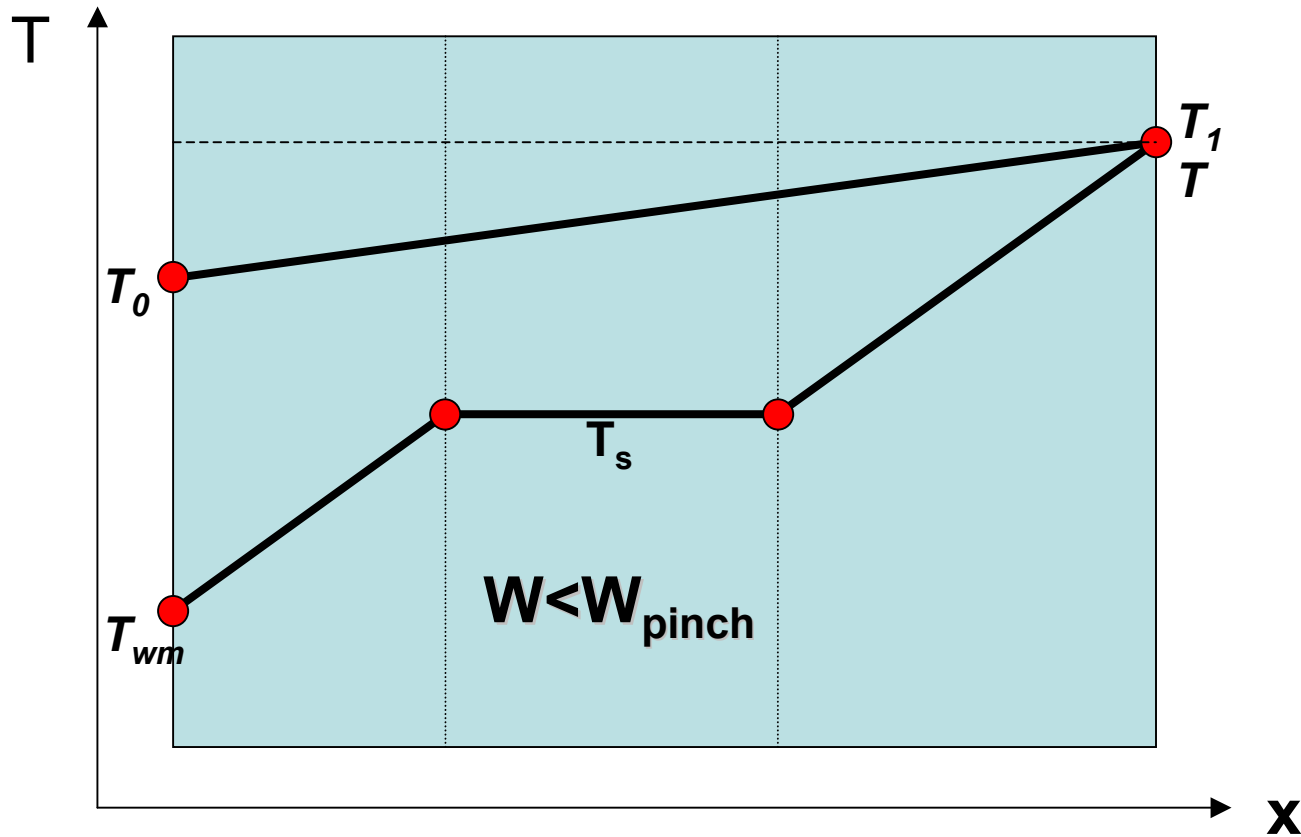
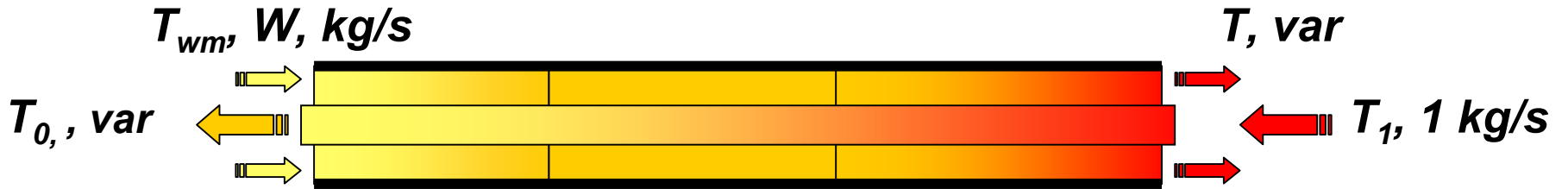
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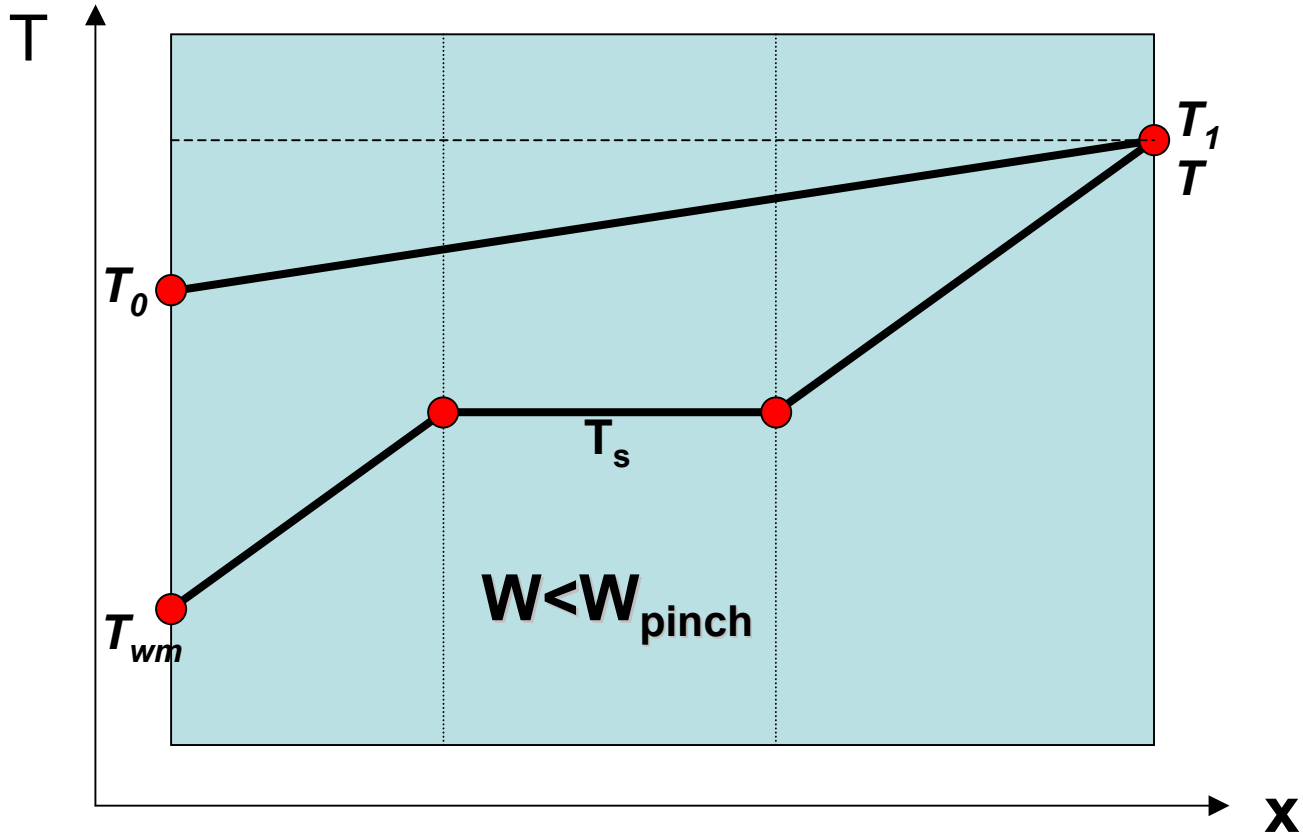
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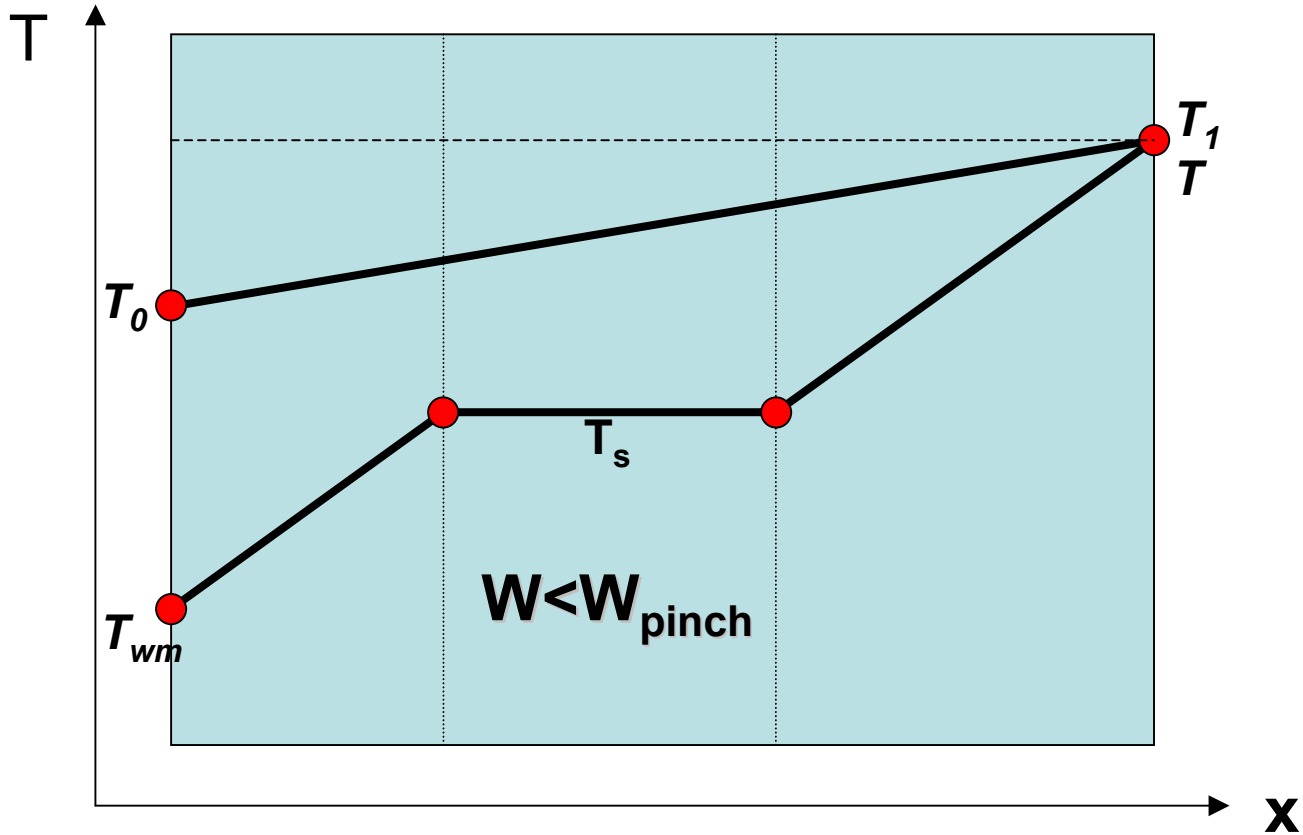
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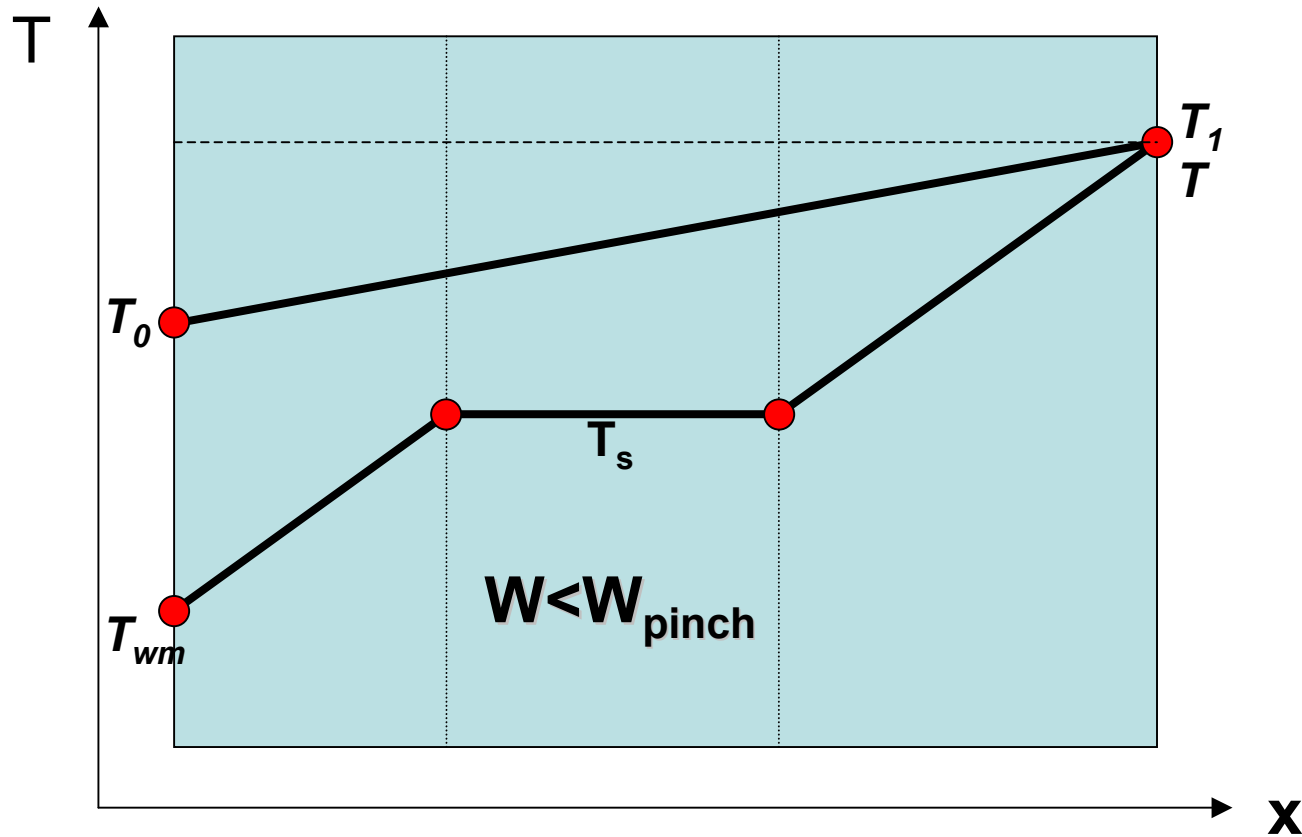
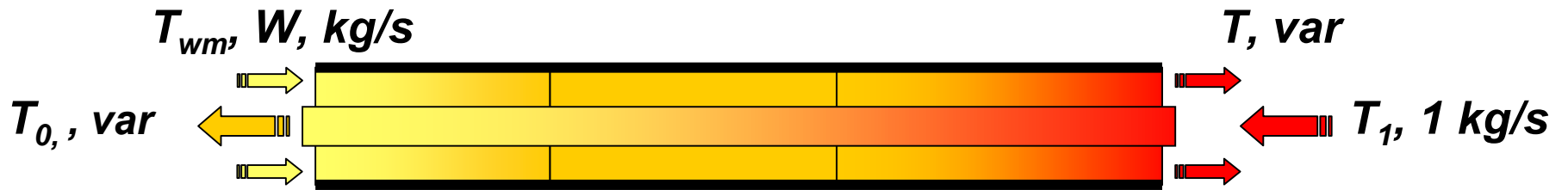
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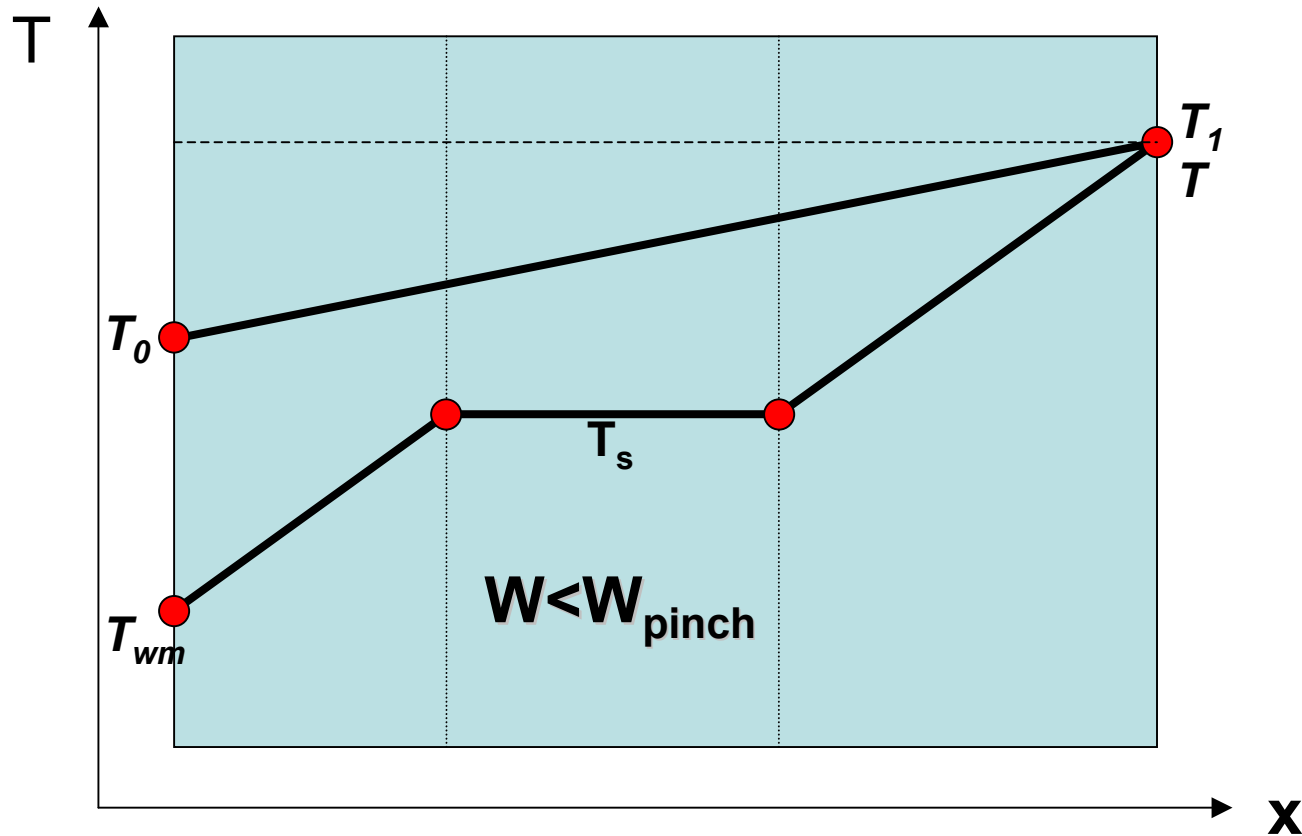
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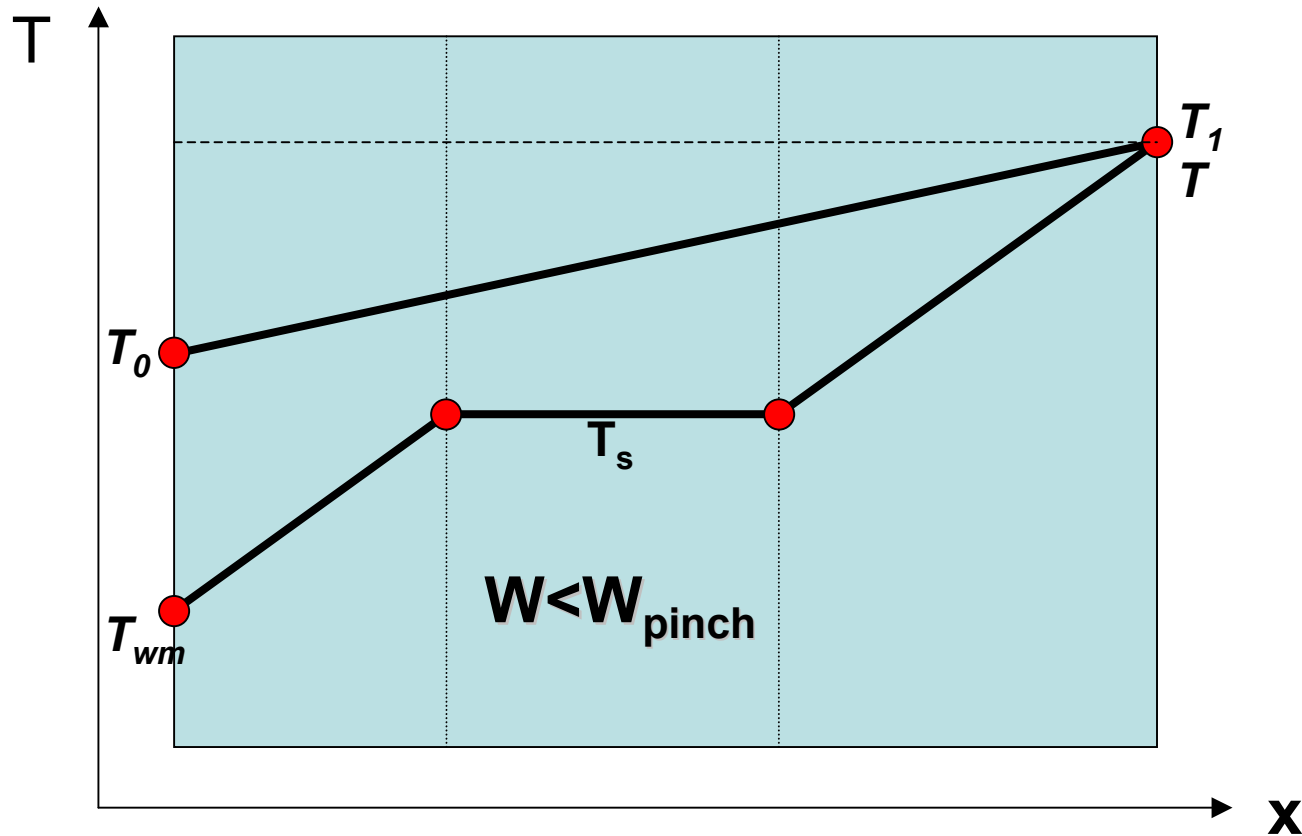
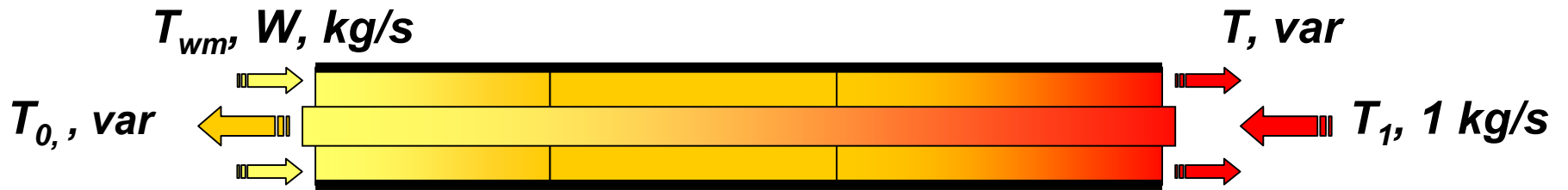
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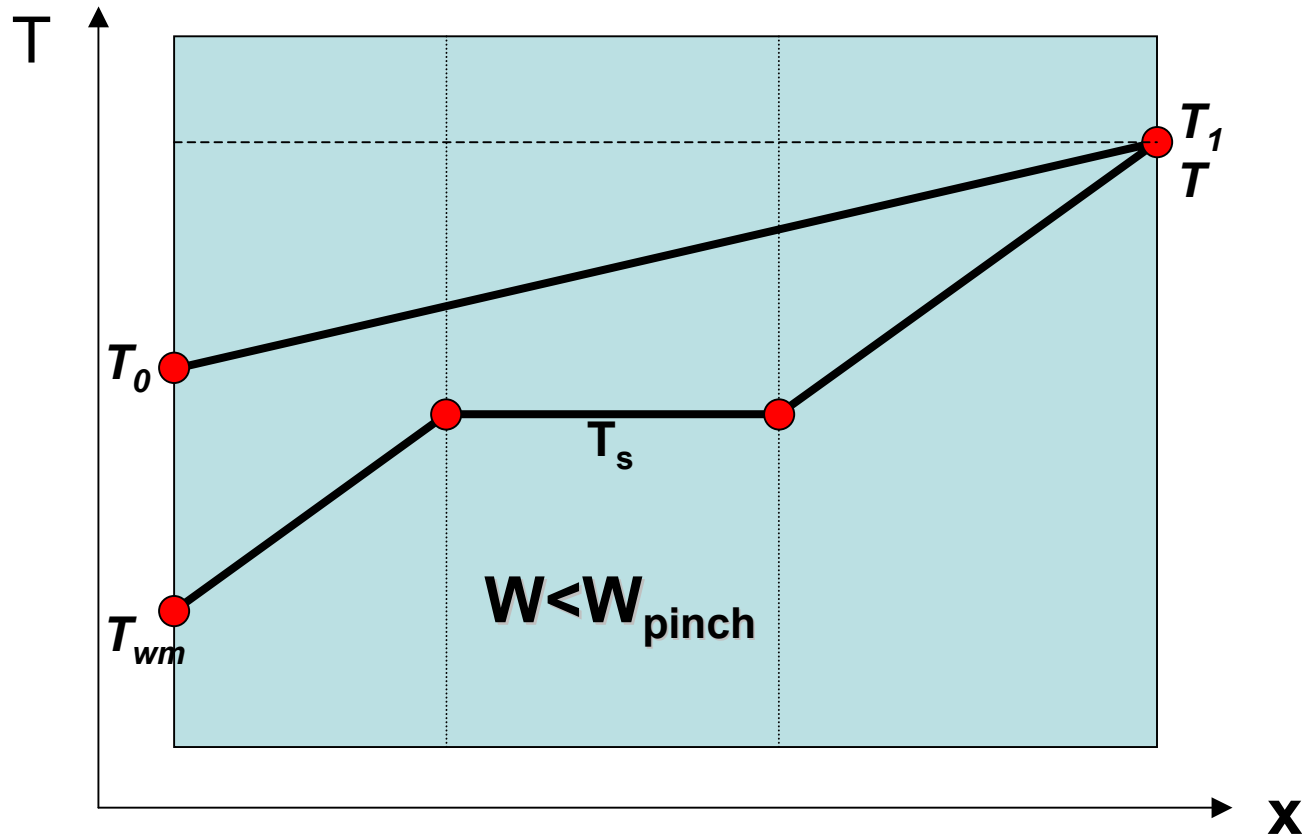
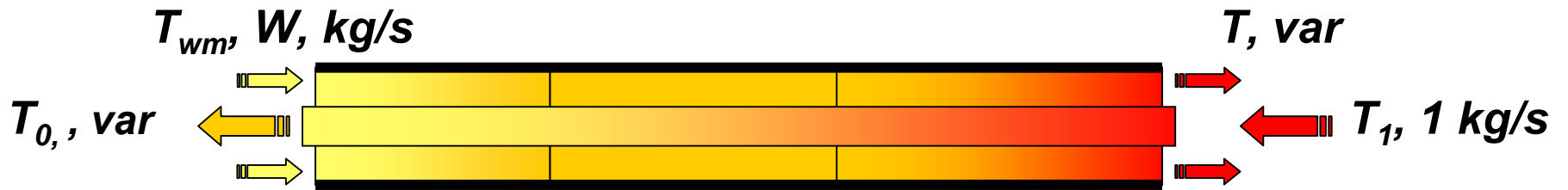
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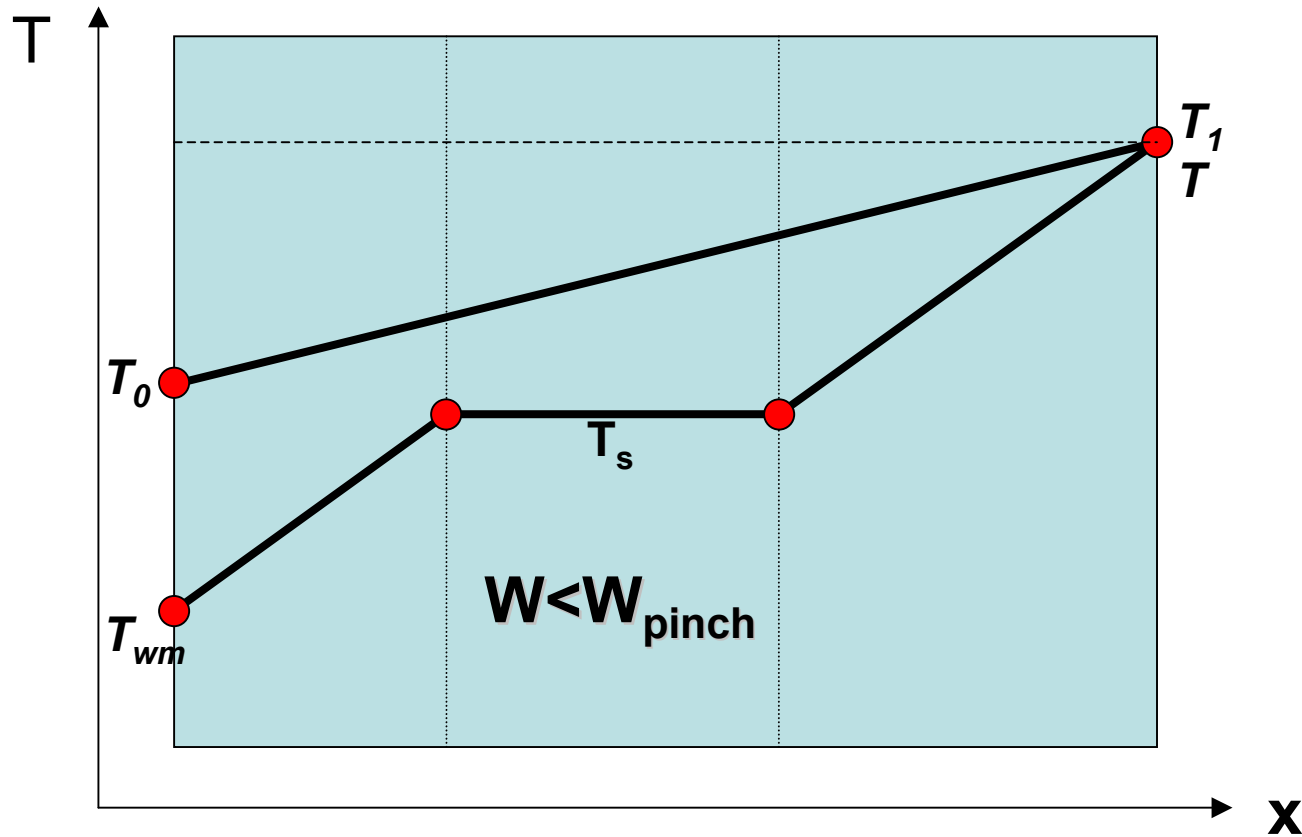
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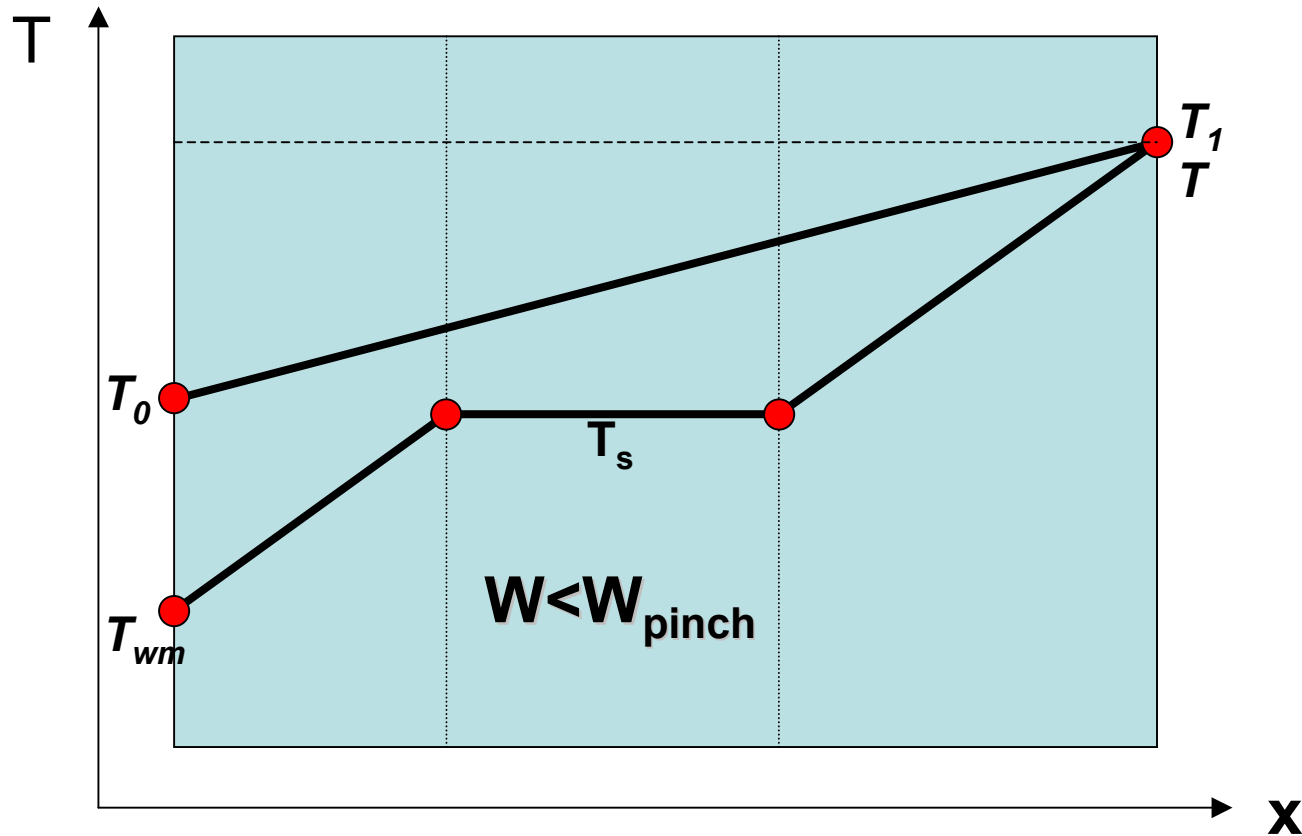
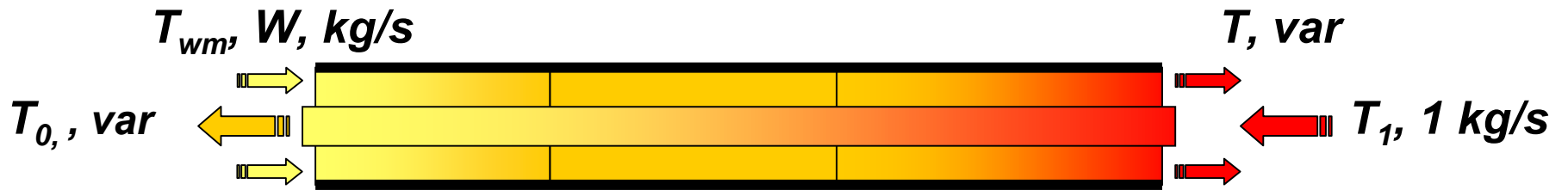
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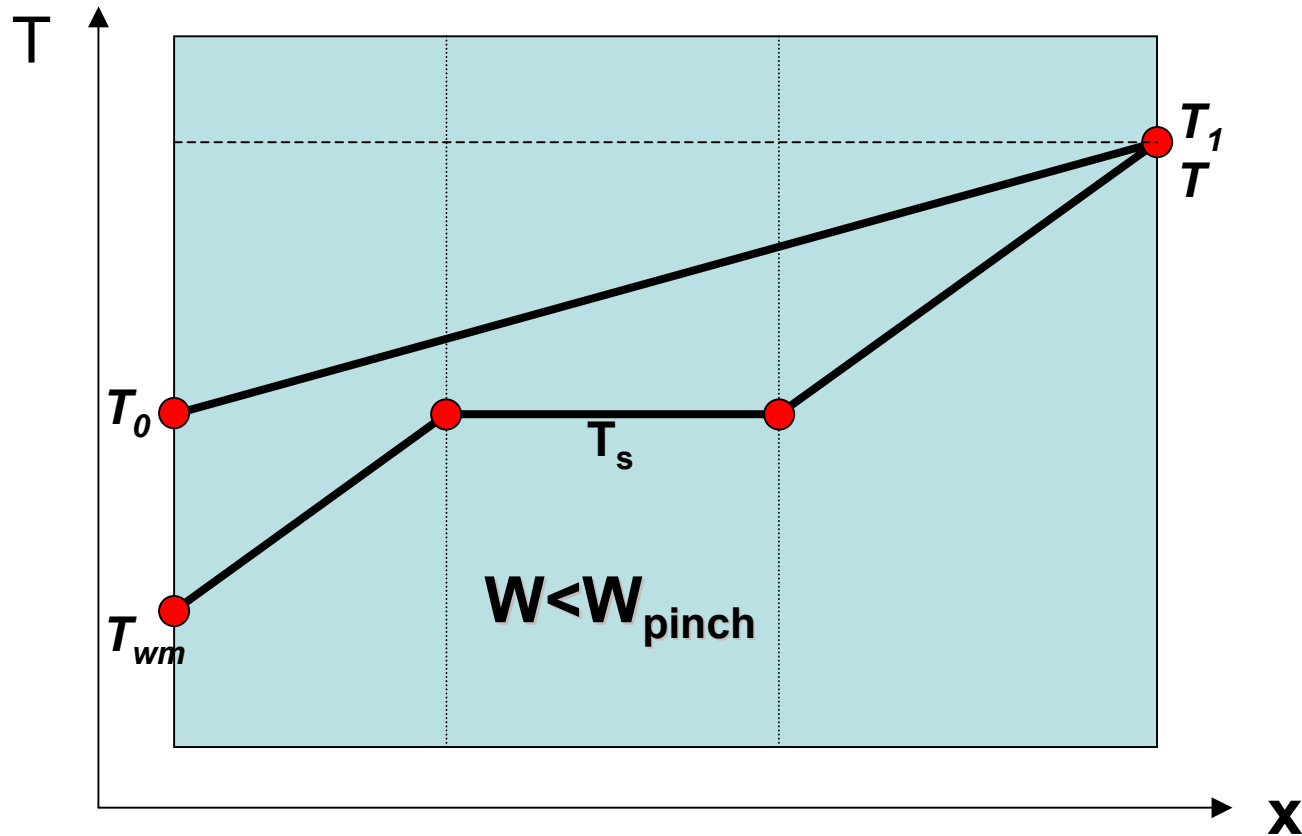
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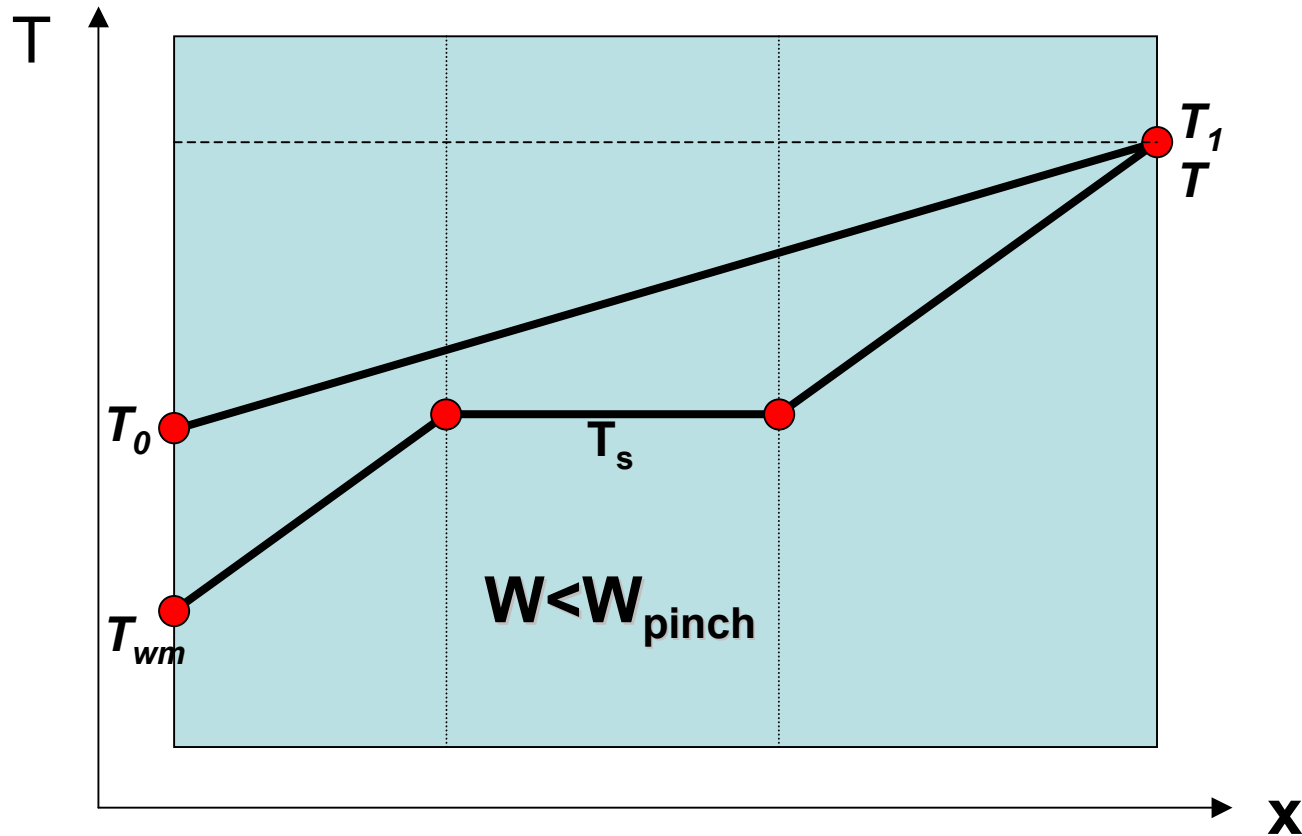
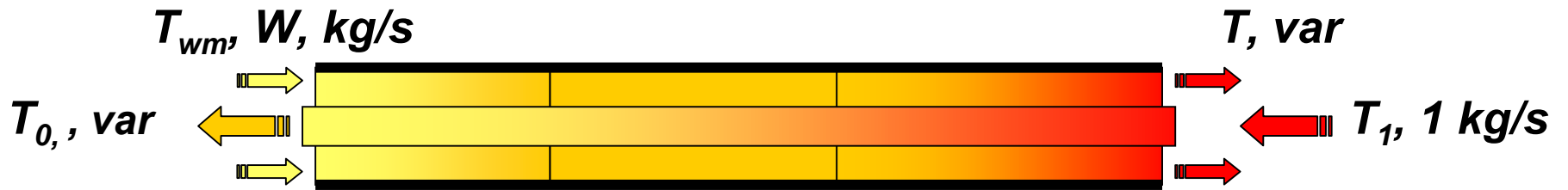
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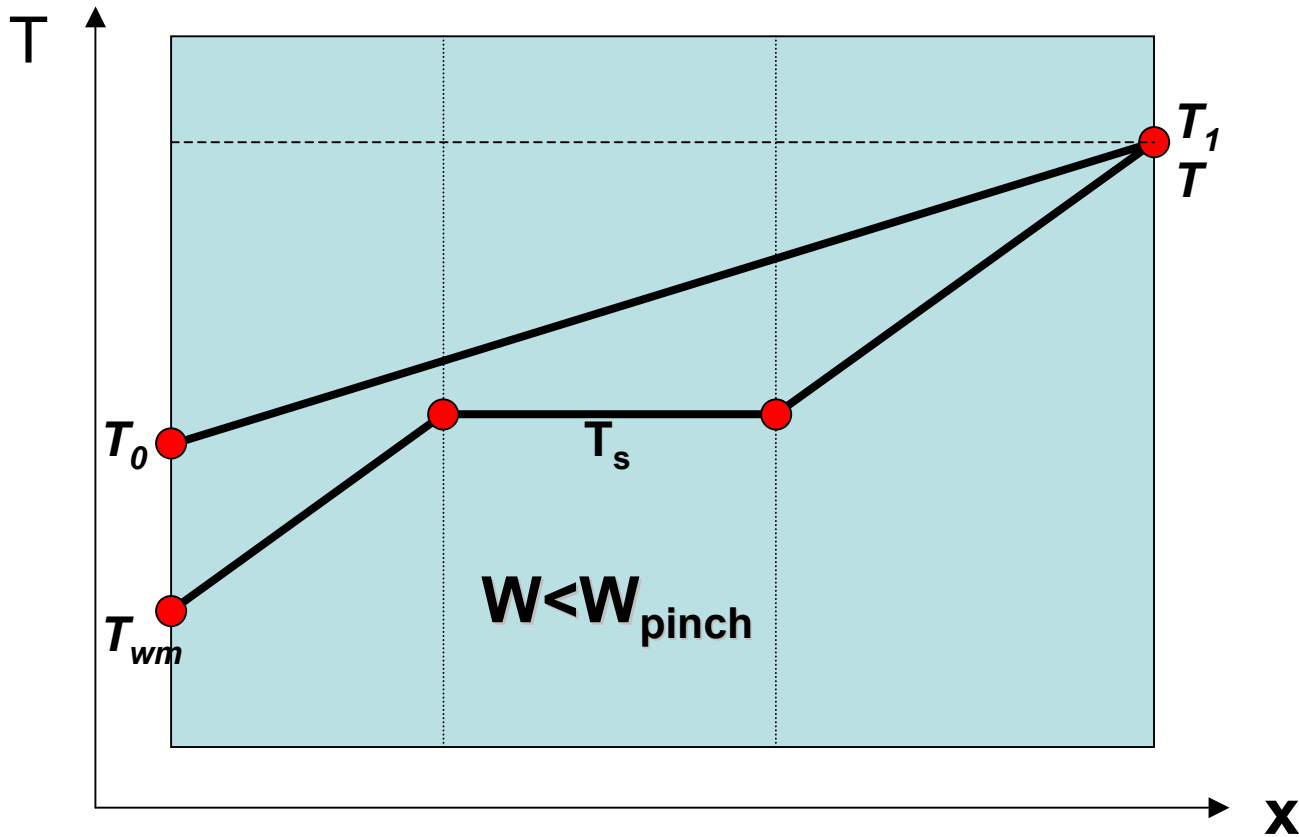
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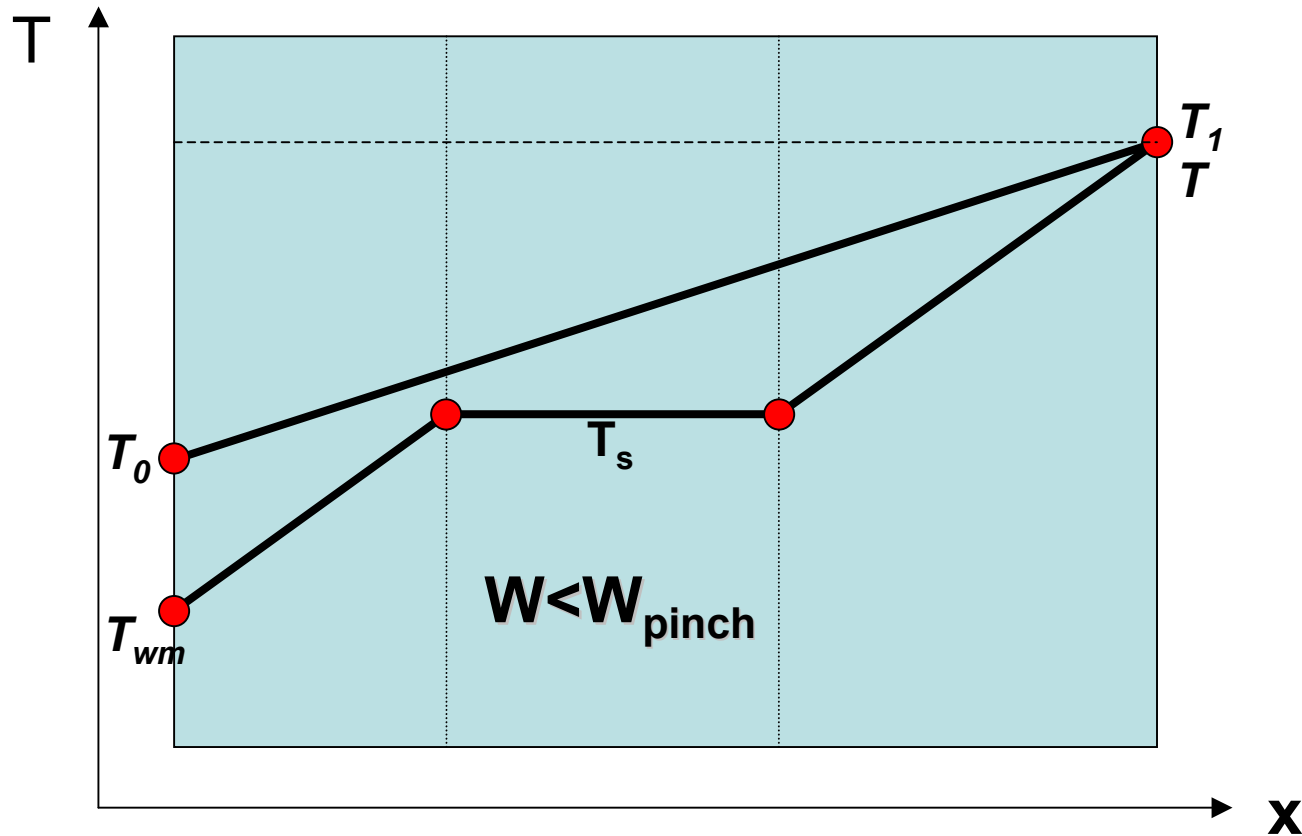
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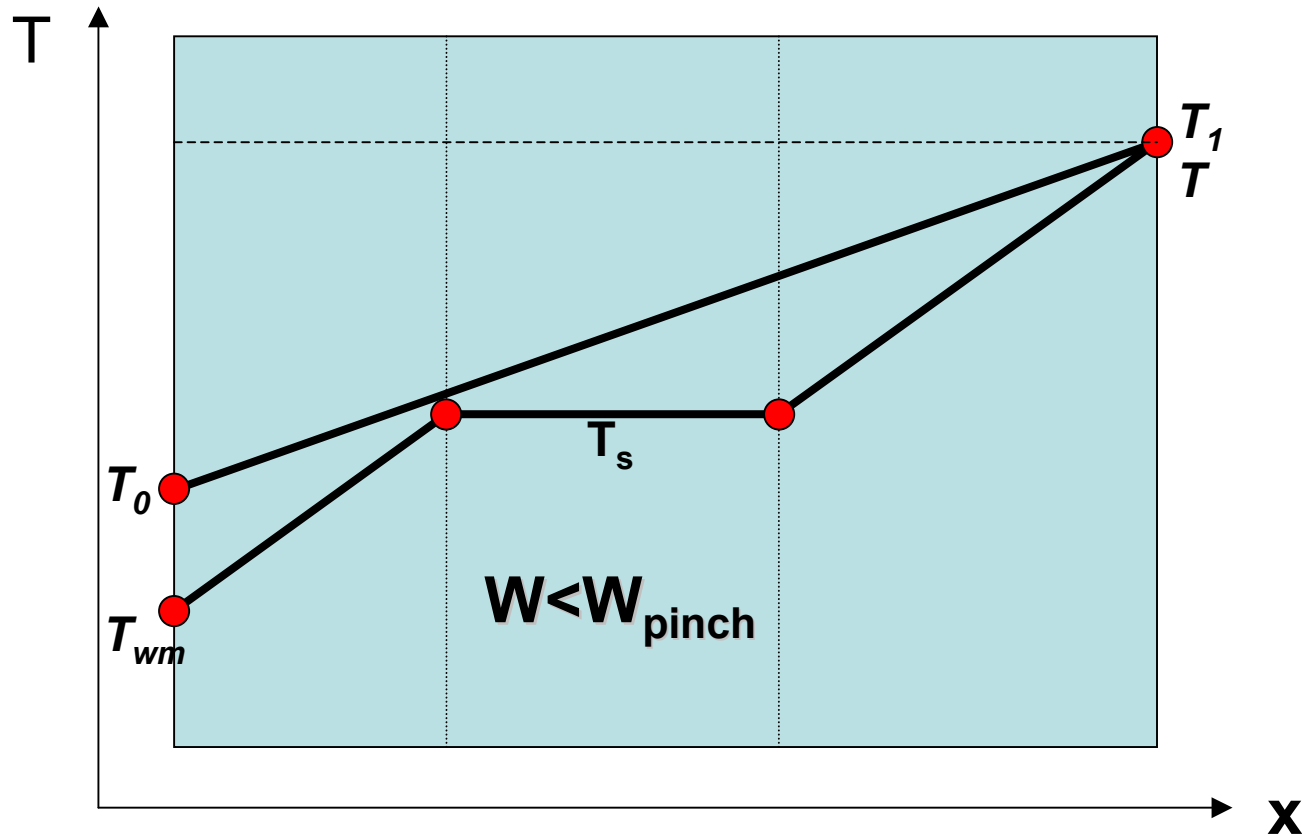
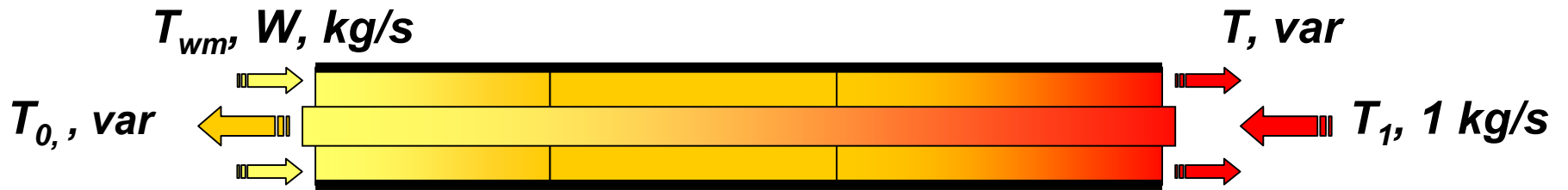
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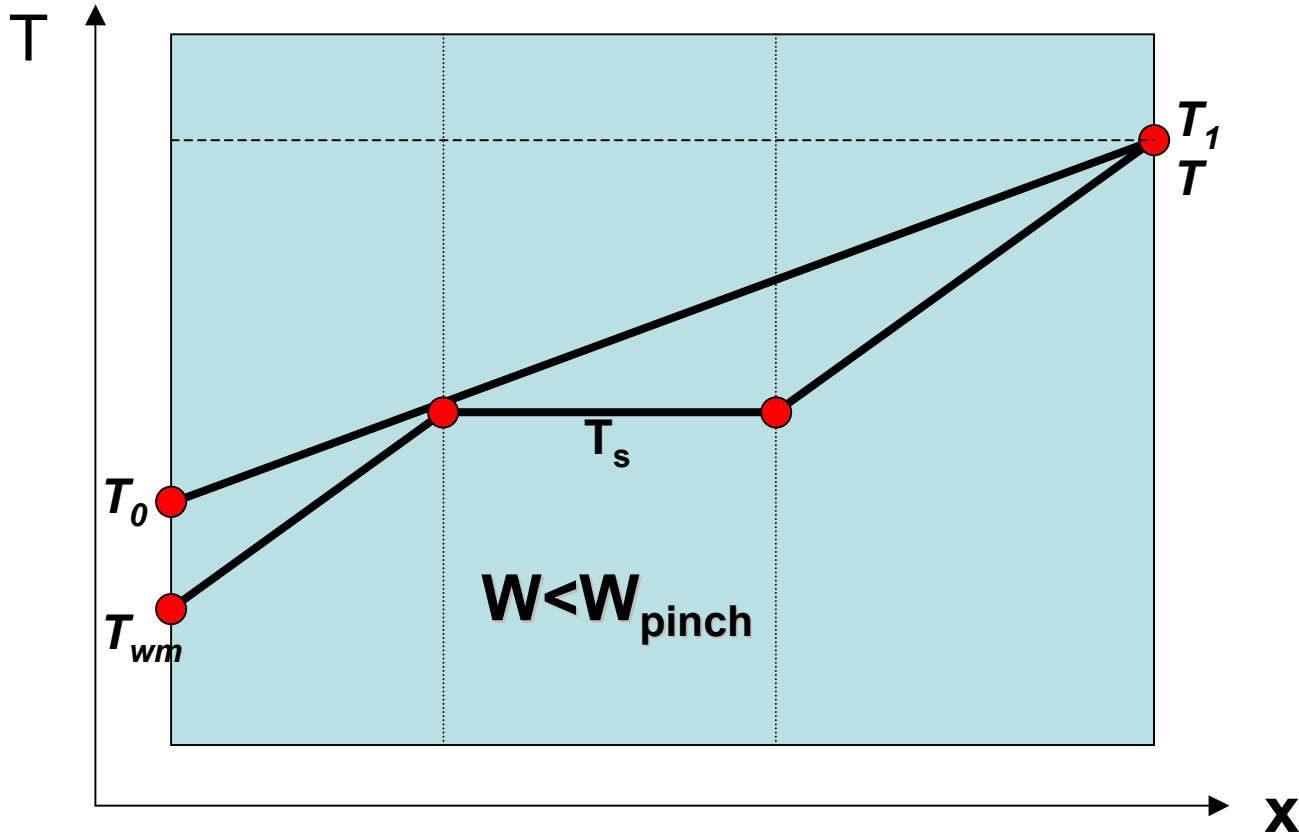
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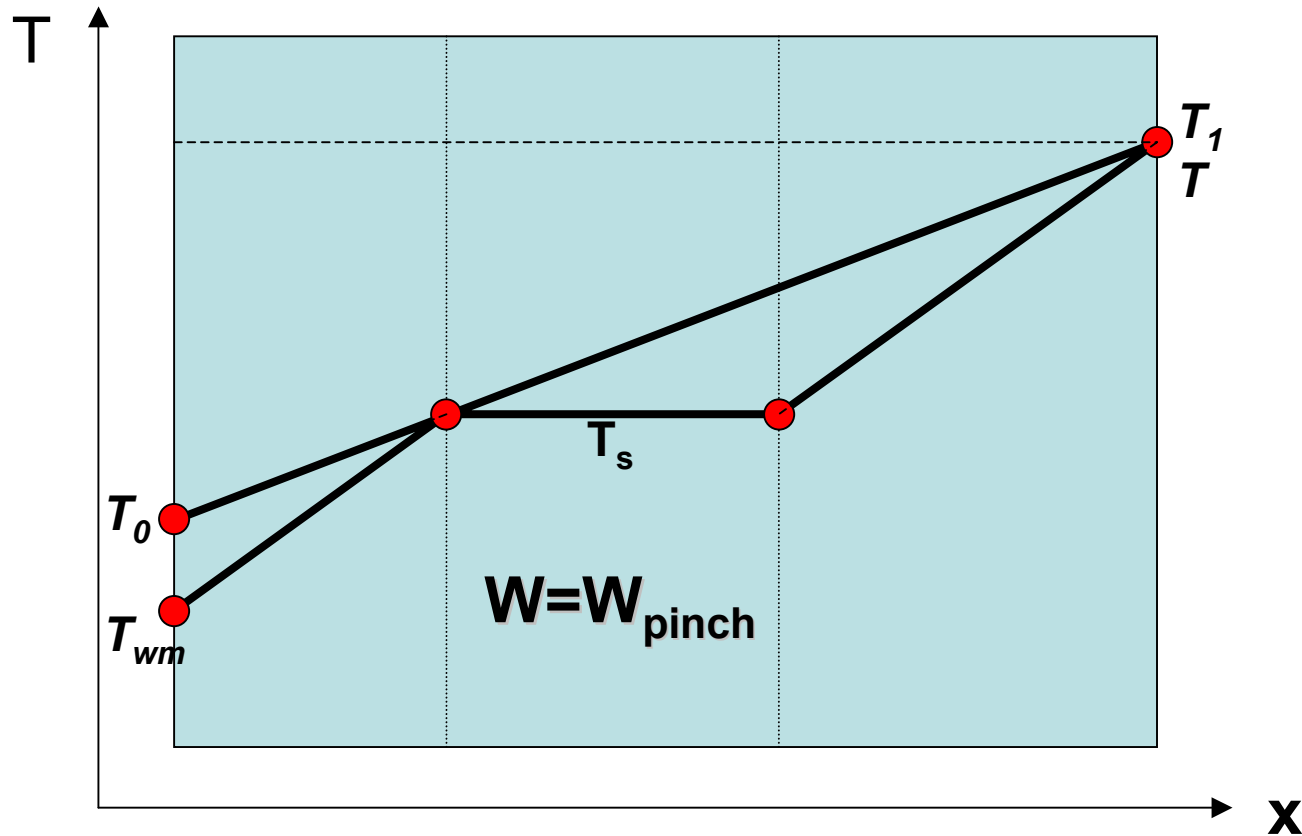
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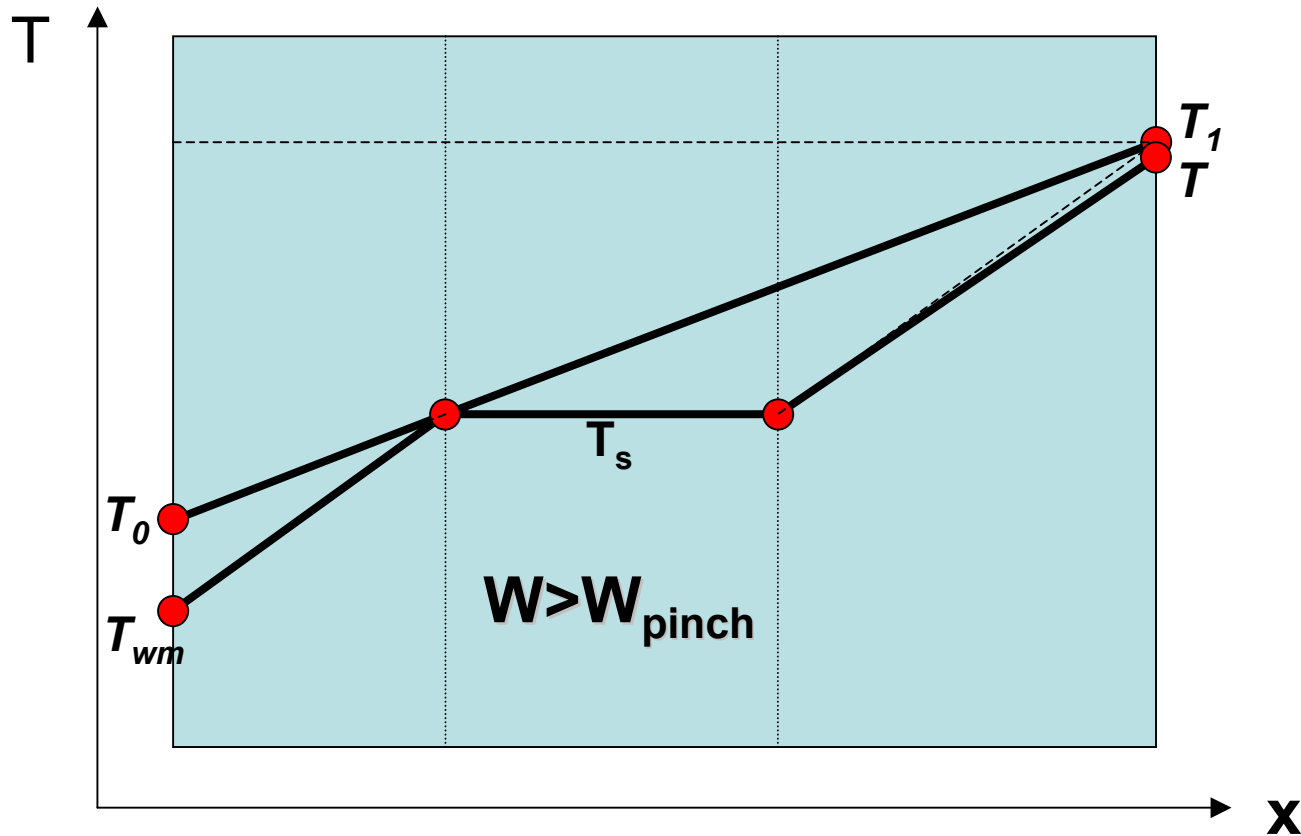
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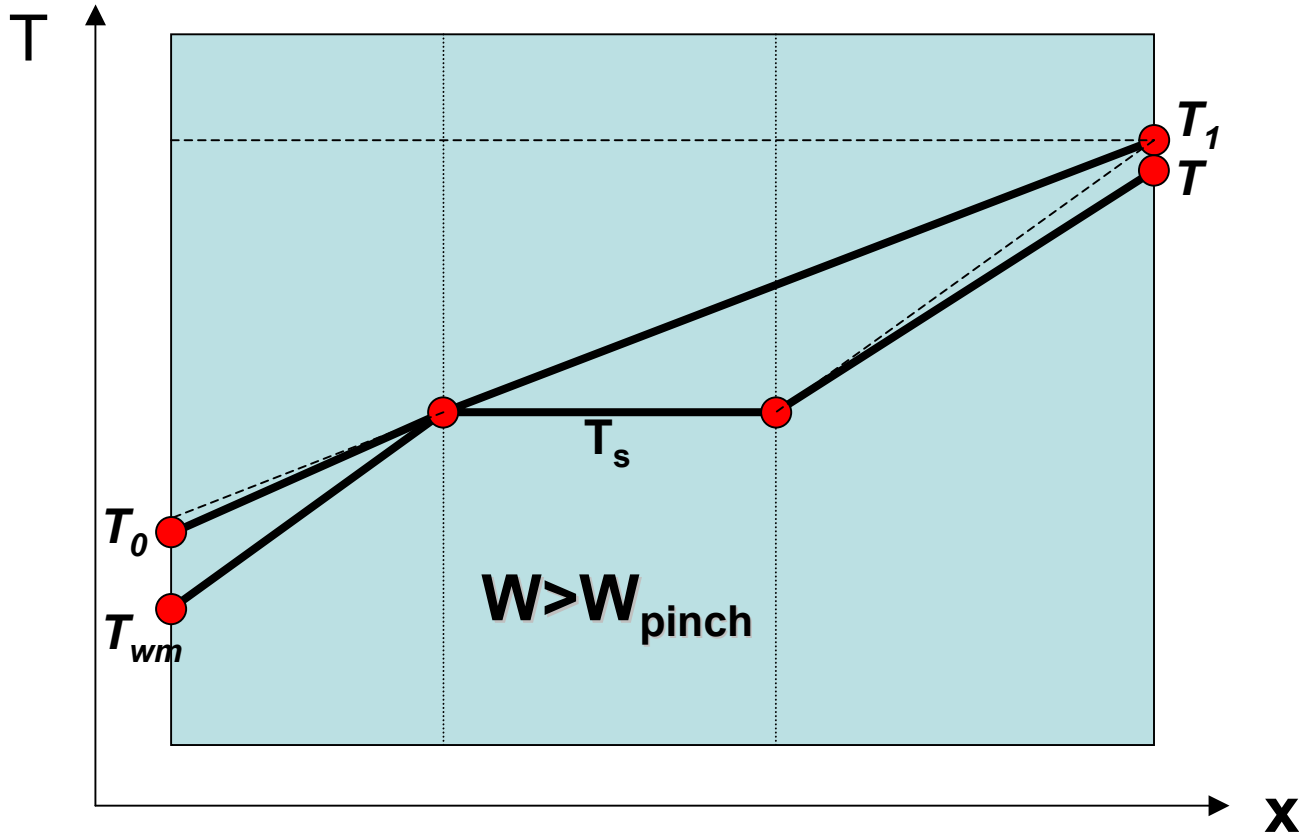
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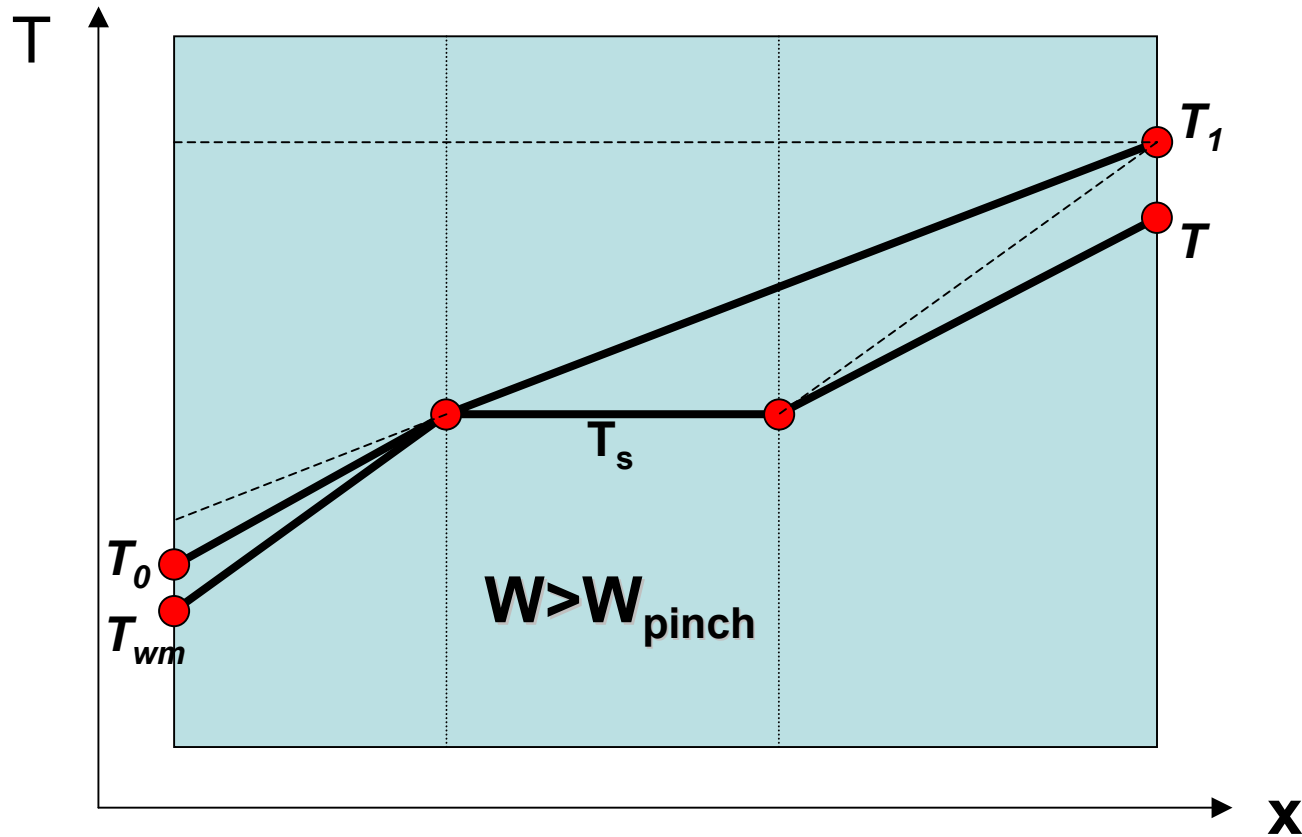
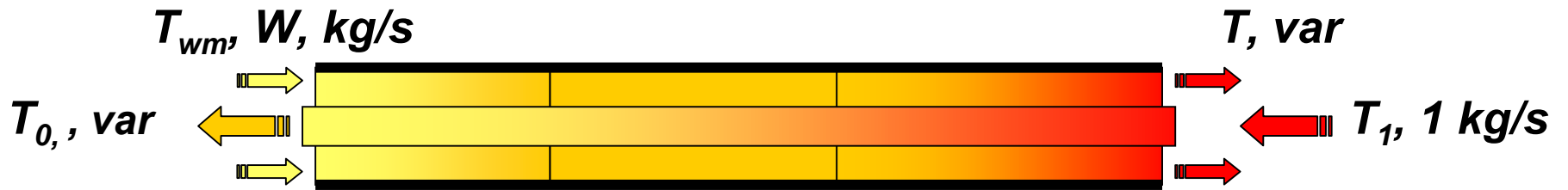
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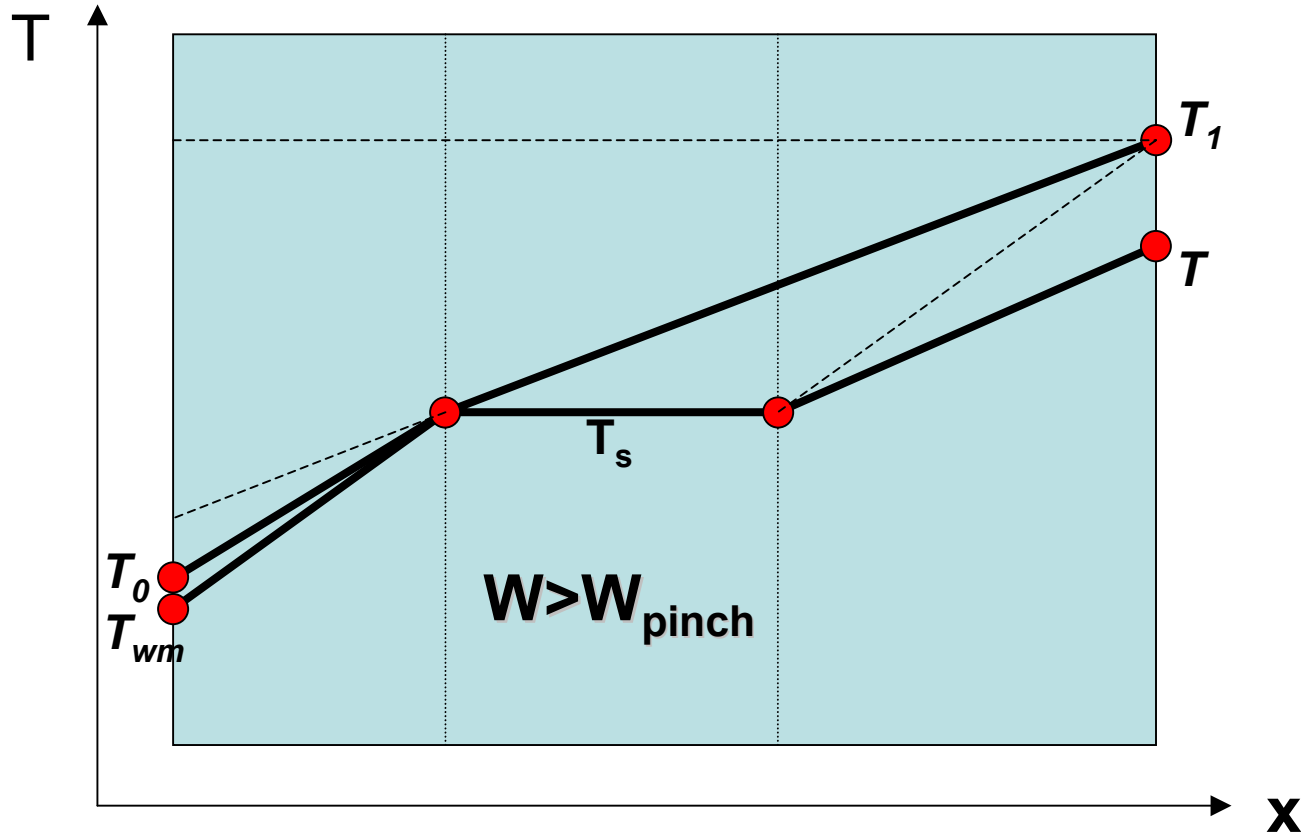
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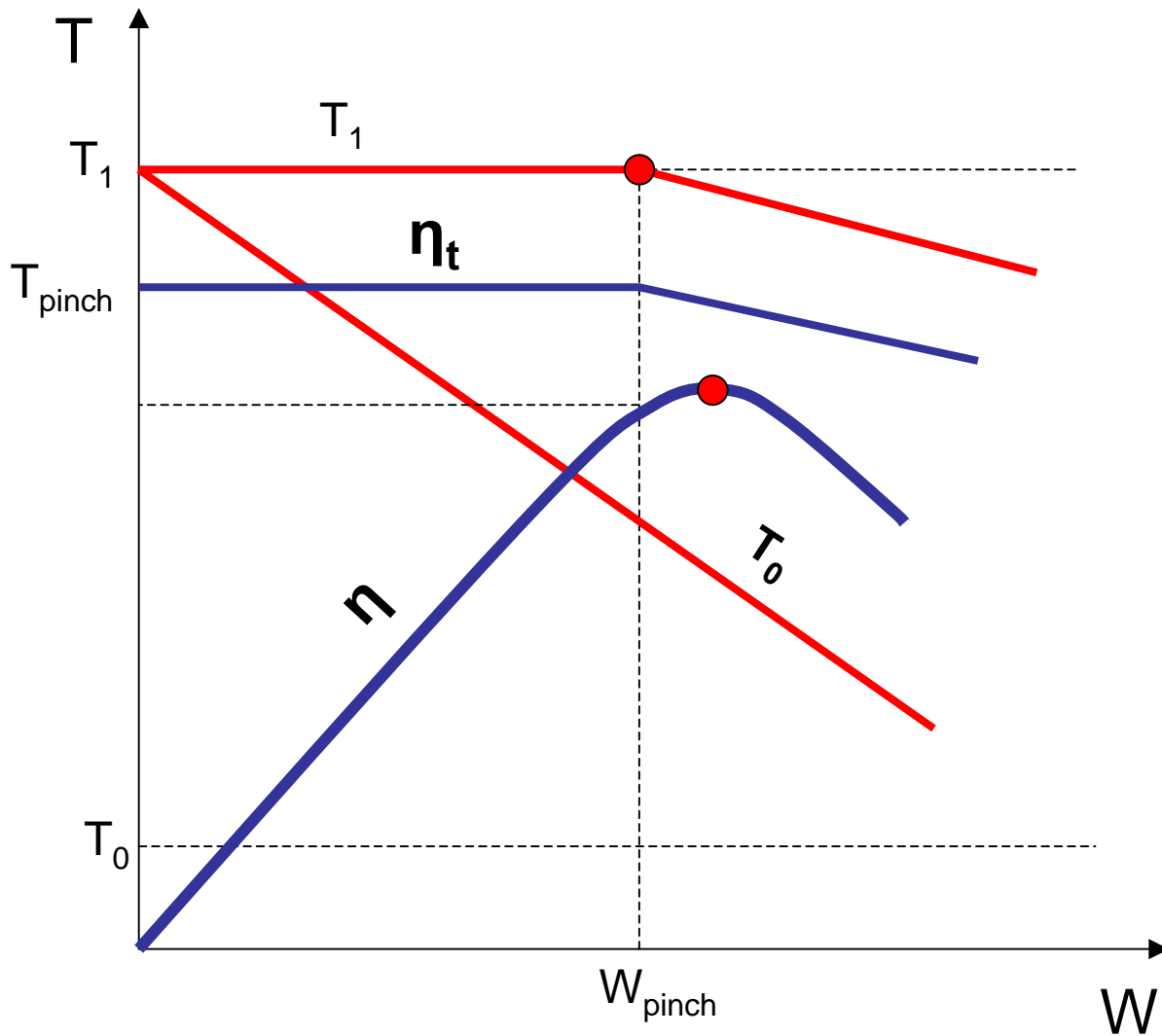
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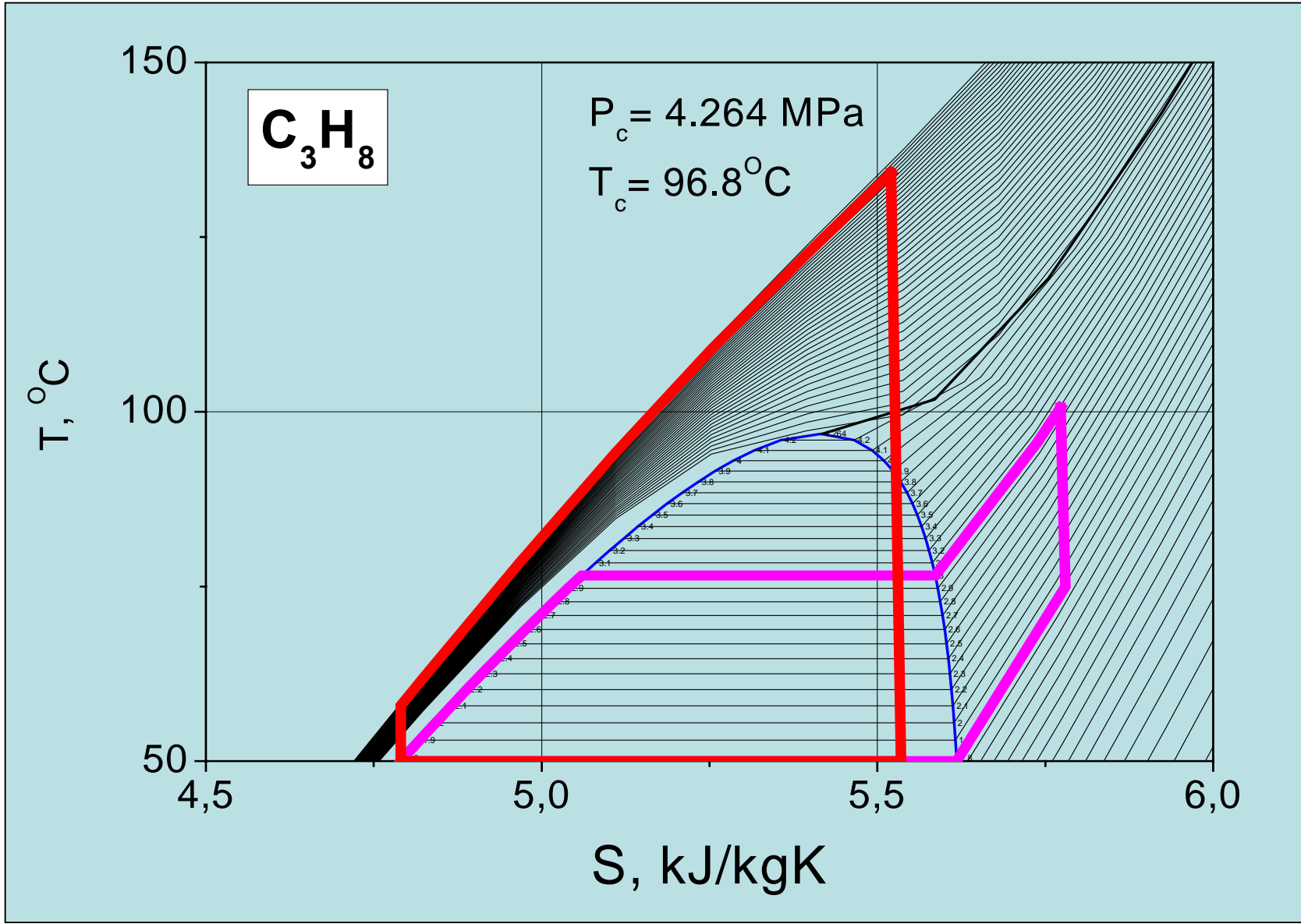
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EFFICIENCY VERSUS FLOW-RATE



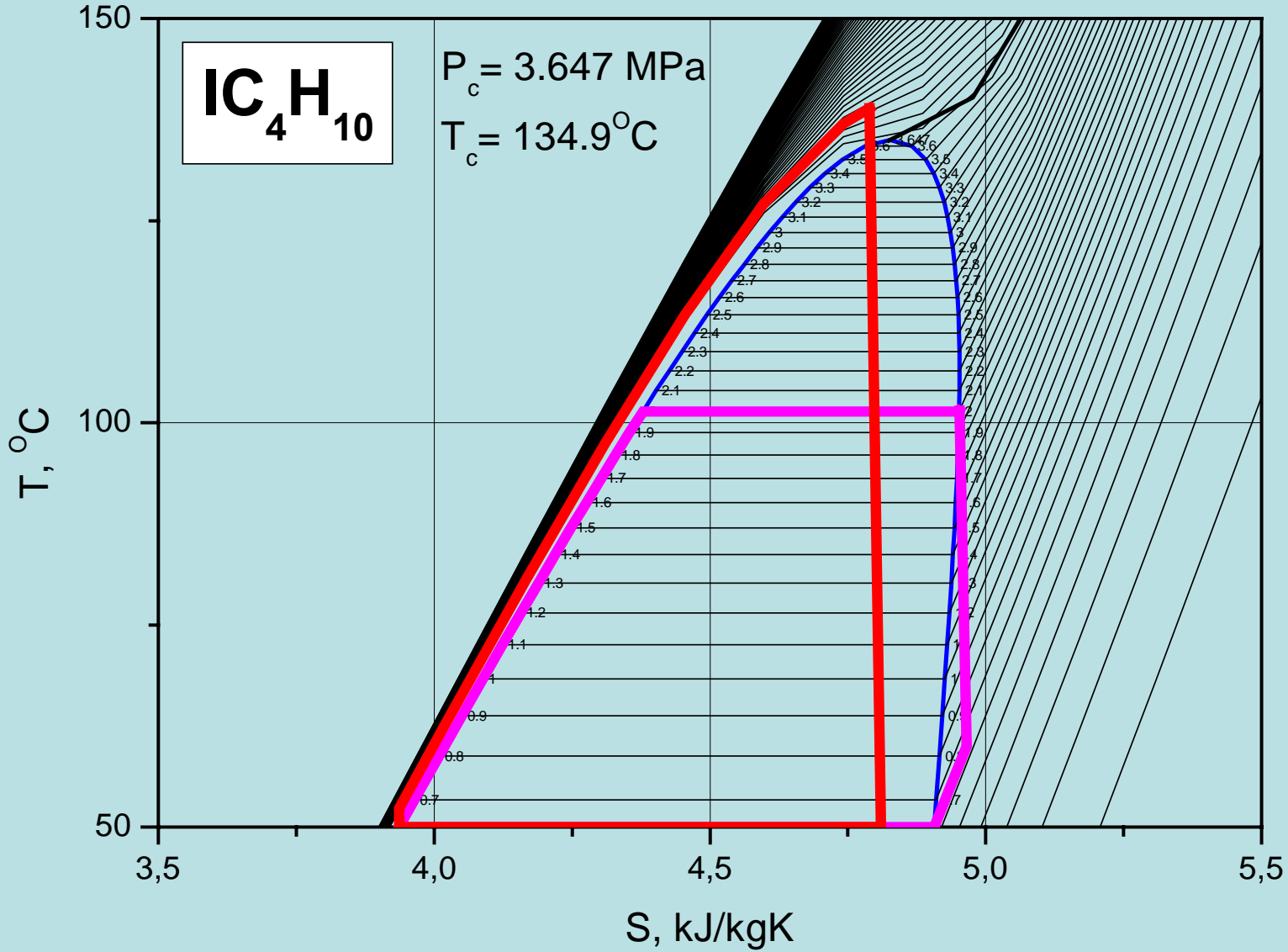
$$\eta = \eta_t \frac{q_1 \times W}{N_{th}}$$



IC₄H₁₀

$P_c = 3.647 \text{ MPa}$

$T_c = 134.9^\circ\text{C}$



CONCLUSIONS:

1. There exist a thermodynamic limit of installation efficiency, defined by the outlet temperature of geothermal water;
2. An optimal thermodynamic cycle should have the heat admission curve similar to the cooling down curve of geothermal water;
3. This condition can be realized with a supercritical Rankine cycle;
4. To provide for maximum installation efficiency it is not enough to maximize the cycle thermal efficiency. It is necessary to look for maximum of the $\eta_t W$ product;
5. The optimal working media flow rate is governed by the temperature pinch in the heat exchanger.